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A New Item Response Theory Model for Estimating Person Ability and Item Parameters for Multidimensional Rank Order Responses

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A New Item Response Theory Model for Estimating Person Ability and Item Parameters
for Multidimensional Rank Order Responses

by

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A dissertation submitted in partial fulfillment
of the requirements for the degree of
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ABSTRACT

The assessment of noncognitive constructs poses a number of challenges that set it apart from traditional cognitive ability measurement. Of particular concern is the influence of response biases and response styles that can influence the accuracy of scale scores. One strategy to address these concerns is to use alternative item presentation formats (such as multidimensional forced choice (MFC) pairs, triads, and tetrads) that may provide resistance to such biases. A variety of strategies for constructing and scoring these forced choice measures have been proposed, though they often require large sample sizes, are limited in the way that statements can vary in location, and (in some cases) require a separate precalibration phase prior to the scoring of forced-choice responses. This dissertation introduces new item response theory models for estimating item and person parameters from rank-order responses indicating preferences among two or more alternatives representing, for example, different personality dimensions. Parameters for this new model, called the Hyperbolic Cosine Model for Rank order responses (HCM-RANK), can be estimated using Markov chain Monte Carlo (MCMC) methods that allow for the simultaneous evaluation of item properties and person scores. The efficacy of the MCMC parameter estimation procedures for these new models was examined via three studies. Study 1 was a Monte Carlo simulation examining the efficacy of parameter recovery across levels of sample size, dimensionality, and approaches to item calibration and scoring. It was found that estimation accuracy improves with sample size, and trait scores and location parameters can be estimated reasonably well in small samples. Study 2 was a simulation examining the robustness of trait estimation to error introduced by substituting subject matter expert (SME) estimates of statement

location for MCMC item parameter estimates and true item parameters. Only small decreases in accuracy relative to the true parameters were observed, suggesting that using SME ratings of statement location for scoring might be a viable short-term way of expediting MFC test deployment in field settings. Study 3 was included primarily to illustrate the use of the newly developed IRT models and estimation methods with real data. An empirical investigation comparing validities of personality measures using different item formats yielded mixed results and raised questions about multidimensional test construction practices that will be explored in future research. The presentation concludes with a discussion of MFC methods and potential applications in educational and workforce contexts.

CHAPTER 1:

INTRODUCTION

The past two decades have shown an increased interest in the assessment of noncognitive constructs due to their ability to predict educational and organizational outcomes beyond cognitive ability alone (Hough & Dilchert, 2010; Viswesvaran, Deller, & Ones, 2007). Constructs such as conscientiousness have been shown to predict both task (Campbell, 1990) and citizenship performance (Borman & Motowidlo, 1997) and may have the advantage of reducing adverse impact that results from the use of measures of cognitive ability (Sackett, Schmitt, Ellingson, & Kabin, 2001). Similarly, in education there is increased interest in examining noncognitive factors, such as academic self-efficacy, need for cognition, and emotional intelligence, and their relationships with educational and achievement outcomes (Richardson, Abraham, & Bond, 2012). Yet another area of interest to researchers is the cross-cultural comparison of relationships between noncognitive constructs and outcomes, such as job performance, educational achievement, and life satisfaction (Diener & Diener, 2009; Frenzel, Thrash, Pekrun, & Götz, 2007; Taras, Kirkman, & Steel, 2010). The inclusion of noncognitive variables in education and organizational research may both increase the prediction efficacy of success in these areas and facilitate understanding of these variables across situational and cultural settings.

Despite these many potential benefits, noncognitive assessment involves a number of challenges that set it apart from cognitive ability assessment. Of particular concern is the influence of response biases and response styles on test scores (McGrath, Mitchell, Kim, &

Hough, 2010; Paulhus, 1991). The predominant approach to measuring noncognitive constructs in organizational and research settings is to present a respondent with a series of descriptors or statements, often transparent as to what is being measured, with instructions to indicate his or her level of agreement (Likert, 1932). This approach has been shown to be susceptible to systematic response biases, with central tendency, extreme response, halo, and socially desirable responding influencing the accuracy of scale scores (Murphy, Jako, & Anhalt, 1993; Van Herk, Poortinga, & Verhallen, 2004). Issues of central tendency and extreme response styles are common in cross cultural research and reduce or distort the relationship between a construct and the outcome of interest (Fischer, 2004). For example, recent research has suggested that cross-cultural differences in response styles may explain the contradictory findings of a positive within-country relationship between self-concept and academic achievement, but a negative relationship when examined between countries (Cheung & Rensvold, 2000; Van da gaer, Grisay, Schulz, & Gebhardt, 2012; Wilkins, 2004). In organizational contexts, socially desirable responding can substantially elevate or depress noncognitive test scores, which particularly alters the rank order of examinees at the extremes of the trait continua and reduces the utility of tests for decision making (Christiansen, Goffin, Johnston, & Rothstein, 1994; Rosse, Stecher, Miller, & Levin, 1998; Stewart, Darnold, Zimmerman, Parks, & Dustin, 2010; Zickar, Rosse, Levin, & Hulin, 1996).

To address these concerns, researchers have examined alternative item presentation formats that may provide resistance to such biases (Borman et al., 2001; Brown & Maydeu-Olivares, 2012; Christiansen, Burns, Montgomery, 2005; Drasgow, Stark, & Chernyshenko, 2011; Heggestad, Morrison, Reeve, & McCloy., 2006; Jackson, 2001; Stark, 2002; Stark, Chernyshenko, & Drasgow, 2005; Stark, Chernyshenko, Drasgow, & White, 2012; Stark,

Chernyshenko, Drasgow, White, Heffner, & Hunter, 2008). Multidimensional forced choice pairs, triads, and tetrads are popular examples. Rather than asking respondents to indicate their level of agreement with individual statements, statements representing different constructs are presented in groups and respondents are instructed to pick or rank the statements in each group from most to least like me (Stark, Chernyshenko, & Drasgow, 2011).

Multidimensional forced choice (MFC) measures have been used across a range of research and applied settings for assessing personality (Stark, Chernyshenko, & Drasgow, 2008; White & Young, 1998), vocational interest (SHL, 2006), and supervisor ratings of job performance (Bartram, 2007; Borman et al., 2001). A number of strategies for constructing and scoring MFC measures have been explored, ranging from summative scoring rules (Hicks, 1970; Hirsh & Peterson, 2008; White & Young, 1998) to those based on factor analytic and item response theory approaches (Maydeu-Olivares & Böckenholt, 2005; Maydeu-Olivares & Brown, 2010; Stark, 2002; Stark et al., 2005). These approaches, however, are not without limitations. Scores obtained through summative strategies cannot be used to make inter-individual comparisons due to the ipsativity resulting from the responses (Baron, 1996; Heggstad et al., 2006; Hicks, 1970; Meade, 2004; Stark, 2002; Stark et al., 2005), and factor analytic and item response theory strategies require large sample sizes and (in some cases) a two-stage approach requiring a separate precalibration of single-statement parameters prior to the scoring of forced-choice responses. Consequently, the application of MFC items in practice and research would benefit from a construction and scoring strategy for which scores can be obtained under conditions of small sample size and potentially streamlined through the incorporation of subject matter expert (SME) ratings into the scale development and scoring process.

The Present Investigation

Forced choice items can vary in their composition and response instructions, resulting in the development of different models to account for the variety of types. Pairwise preference models have been developed for unidimensional item responses (e.g., Andrich, 1995; Stark & Drasgow, 2002; Zinnes & Griggs, 1974) and multidimensional pairs (e.g., Stark et al., 2005; Zinnes & Griggs, 1974), in addition to models for item tetrads (e.g., Brown & Maydeu-Olivares, 2011; Brown & Maydeu-Olivares, 2013; de la Torre, Ponsoda, Leenen, & Hontangas, 2012). Although recent research has made significant advances in the scoring of these items, there is still a need for a model which can address a range of MFC formats, has item and person parameters which can be efficiently estimated, and that can be easily implemented in applied settings.

This paper will introduce a model for estimating item and person parameters from data collected via the rank-ordering of statements presented in a MFC format. Working from Luce's (1959) theory of choice behavior, the Hyperbolic Cosine Model (HCM; Andrich & Luo, 1993) for single-stimulus data will be extended to the multidimensional forced choice case. This new model, called the Hyperbolic Cosine Model for Rank order responses (HCM-RANK), provides the basis for the recovery of both person trait estimates and item parameter estimates directly from rank-order responses. A special case of this model, the Simple HCM-RANK (SHCM-RANK), is particularly attractive because each statement in a forced choice item is represented by just one location or extremity parameter, which might be estimated using subject matter experts (SMEs) judgments in the early stages of testing.

The following chapters will provide an overview of the use of forced choice measures in noncognitive assessment and the methods that have been developed for scoring and item

analysis. Next, recent advances in the scoring of MFC items and assumptions about the underlying response process will be reviewed. The HCM as a model for single-stimulus (i.e., single statement) responses will be described, and the HCM-RANK model for MFC rank responses will be derived. Following a detailed description of the HCM-RANK parameter estimation procedures, Study 1 will explore parameter recovery using a Monte Carlo simulation that varies sample size, dimensionality, and approaches to item calibration and scoring. A second simulation, Study 2, will examine the robustness of trait score estimation to error introduced by substituting subject matter expert (SME) estimates of statement location for true parameters. Study 3 will illustrate the use of the newly developed IRT models and MCMC estimation methods with real data, and the presentation will conclude with a discussion of potential MFC applications in educational and workforce contexts.

CHAPTER 2:

APPROACHES TO SCORING FORCED CHOICE MEASURES

Forced choice measures have been explored by applied psychologists for noncognitive testing since the late 1930s (e.g., Strong Vocational Interest Blank, Strong, 1938; Gordon Personal Profile, Gordon, 1953). However, concerns about ipsativity have, until recently, impeded widespread use in organizations. Classical test theory methods of scoring, in which a point is awarded for endorsing an option in a forced choice item, generally lead to ipsative data characterized by total scores that sum to a constant across dimensions and negative scale correlations (Hicks, 1970; Meade, 2004; Stark, 2002; Stark, Chernyshenko, & Drasgow, 2005). However, research over the last two decades has produced several efficacious ways of deriving normative information from multidimensional forced choice (MFC) measures (Brown & Maydeu-Olivares, 2011; de la Torre et al., 2012; Stark, Chernyshenko, & Drasgow, 2005), and research showing that MFC measures are more resistant than single statement measures to response biases, such as rating scale errors (Borman et al., 2001) and socially desirable responding (Jackson, Wroblewski, & Ashton, 2000; Stark, Chernyshenko, Drasgow, White, Heffner, & Hunter, 2008; Stark, Chernyshenko, & Drasgow, 2010; Stark, Chernyshenko, & Drasgow, 2011), has reinvigorated interest for personnel screening applications.

Classical Test Theory Methods

Beginning in the mid-1990s, there were several key research developments that laid the foundation for modern MFC testing and the research conducted for this dissertation. The first breakthrough came from the U.S. Army Research Institute's Assessment of Individual

Motivation (AIM) research program. The AIM inventory measures six dimensions of personality using MFC tetrads that require a respondent to pick the one statement in each tetrad that is “most like me” and the one that is “least like me.” The response data for each tetrad are coded trichotomously, with scores of 1 being assigned to unselected options and scores of 0 or 2 being assigned to selected options based on how the statements are keyed. As described by White and Young (1998), this classical test theory method of scoring produces data that are only partially ipsative (Hicks, 1970), which allows interindividual score comparisons for personnel screening applications. An example MFC tetrad from Young et al. (2004) is shown below.

- ___ (A) I have almost always completed projects on time.
- ___ (B) I have not exercised regularly.
- M (C) I have enjoyed coordinating the activities of others.
- L (D) I have a hard time feeling relaxed before an important test.

Research involving MFC measures, constructed and scored in ways similar to the AIM, have generally produced positive findings in terms of scale reliabilities, intercorrelations, and validities relative to single-statement measures (Dragow, Lee, Stark, & Chernyshenko, 2004; Young et al., 2004). One limitation of this approach, however, is that is not amenable to computer adaptive testing, which is becoming increasingly important in organizational settings because of the need to assess more constructs in the same or shorter periods of time. In addition, classical test theory methods provide limited information for building parallel forms and comparing psychometric properties across different subpopulations of respondents. Consequently, researchers embarked on addressing these issues from different perspectives.

Stark, Chernyshenko, and Drasgow developed an item response theory (IRT) approach to MFC test construction and scoring using a multidimensional pairwise preference format, which requires respondents to choose the one statement in each pair that is more like me (Stark, 2002; Stark, Chernyshenko, & Drasgow, 2005; Stark, Chernyshenko, Drasgow, & White, 2012). Böckenholt (2001, 2004) developed confirmatory factor analytic (CFA) methods for scoring unidimensional pairwise preference items, and Maydeu-Olivares and Brown (2010) began developing CFA methods for constructing and scoring MFC tests involving more complex item formats, such as triads or tetrads (e.g., OPQ32i; SHL, 2006), which require respondents to rank response alternatives from most to least like me. Later, de la Torre, Ponsada, and colleagues (2012) generalized Stark's (2002) approach for use with more complex formats and developed Markov chain Monte Carlo (MCMC) estimation methods for simultaneously calibrating and scoring MFC items, which facilitates traditional IRT methods of item analysis, equating, and differential item functioning detection.

The remainder of this chapter describes the Stark et al. and Maydeu-Olivares and Brown approaches to MFC test construction and scoring. The next chapter describes de la Torre et al.'s models for MFC responses, which subsume Stark's (2002) model as a special case. Following are several chapters devoted to the topic of this dissertation. In short, I describe the development and evaluation of a new model for MFC testing applications, which capitalizes on the technological advances attributable to de la Torre et al., while incorporating features that may ultimately improve and accelerate the process of MFC test development and launch for organizational applications.

The Multi-Unidimensional Pairwise Preference Model

Stark (2002) proposed an IRT method for MFC test construction and scoring that was designed to overcome ipsativity and provide a foundation for computerized adaptive testing applications. Rather than using item tetrads, he adopted a pairwise preference format because it was a logical extension of the unidimensional pairwise preference research conducted previously in the context of performance appraisal (Borman et al., 2001; Stark & Drasgow, 2002) and it was more mathematically tractable for this initial foray into IRT MFC test construction and scoring. Pairwise preference items were also selected to simplify the response process for participants, because research underway at the time suggested that tetrads have a higher “cognitive load,” which may cause examinee fatigue and potentially reduce the incremental validities over cognitive ability measures (Böckenholt, 2004; Christiansen, Burns, Montgomery, 2005; Converse, Oswald, Imus, Hedricks, Roy, & Butera, 2008; Vasilopoulos, Cucina, Dyomina, Morewitz, & Reilly, 2006).

Stark’s model, now referred to as the multi-unidimensional pairwise preference model (MUPP; Stark, Chernyshenko, & Drasgow, 2005), assumes that when presented with a pair of statements, representing the same or different constructs, a respondent evaluates each statement and makes independent decisions about agreement. Formally, the probability of preferring statement s to statement t in a pairwise preference item is given by:

$$P(s > t)_i(\theta_{d_s}, \theta_{d_t}) = \frac{P_{st}\{1,0\}}{P_{st}\{1,0\} + P_{st}\{0,1\}} = \frac{P_s(1)P_t(0)}{P_s(1)P_t(0) + P_s(0)P_t(1)}, \quad (2.1)$$

where:

i = the index for each pairwise preference item, where $i = 1$ to I ;

s, t = the indices for the first and second statements, respectively, in an item;

d = the dimension associated with a given statement, where $d = 1, \dots, D$;

$\theta_{d_s}, \theta_{d_t}$ = the latent trait values for a respondent on dimensions d_s and d_t , respectively;

$P_{st}\{1,0\}$ = the joint probability of selecting statement s , and not selecting statement t ;

$P_{st}\{0,1\}$ = the joint probability of selecting statement t , and not selecting statement s ;

$P_s(1), P_t(1)$ = the probabilities of endorsing statements s and t , respectively;

$P_s(0), P_t(0)$ = the probabilities of not endorsing statements s and t , respectively; and

$P(s > t)_i(\theta_{d_s}, \theta_{d_t})$ = the probability of a respondent preferring statement s to statement t in pairwise preference item i .

This formulation of pairwise preference probability is notably similar to Andrich's (1995) definition for unidimensional pairwise preferences.

Stark (2002) described and evaluated a two-stage approach to MFC test construction and scoring. First, write noncognitive statements ranging in extremity from low to medium to high on the constructs to be assessed. Administer the statements to large samples of respondents with instructions to indicate their levels of agreement using an ordered polytomous response format. Dichotomize the polytomous data and estimate statement parameters using an IRT model for single-statement responses that provides adequate model-data fit. Based on research at the time, Stark chose the Generalized Graded Unfolding model (Roberts, Donoghue, & Laughlin, 2000) as the basis for test construction and scoring, although many other ideal point and dominance models could have been selected. After estimating statement parameters using the GGUM, obtain social desirability ratings for MFC item creation by re-administering the statements in the context of a "fake good" study (White & Young, 1998) or by collecting subject matter expert ratings. Next, form multidimensional pairwise preference items by pairing statements similar in

social desirability from different dimensions, and assemble MFC test forms by combining multidimensional pairs with a small percentage of similarly matched unidimensional pairs to identify the metric of trait scores. Scoring multidimensional pairwise preference tests is then accomplished by multidimensional Bayes modal estimation, via the substitution of observed responses and GGUM statement parameters into Equation 2.1 for pairwise preference response probabilities. For future adaptive testing applications, Stark (2002) provided item and test information equations that could be used to create and select items that are optimal for individual examinees, subject to content constraints, at any point during an exam.

Stark (2002) and Stark, Chernyshenko, and Drasgow (2005) conducted Monte Carlo simulations to examine trait score recovery with MFC tests of different lengths, dimensionality, and percentages of unidimensional pairings. Overall, they found good to excellent recovery of trait scores with 20% or fewer unidimensional pairings, but the standard errors produced by the multidimensional minimization procedure were too conservative. Stark, Chernyshenko, Drasgow, and White (2012) reported follow-up simulations comparing nonadaptive and adaptive MFC testing with as many as 25 dimensions and, consistent with expectations, they found that adaptive testing yielded trait score recovery statistics comparable to nonadaptive tests that were nearly twice as long, scoring was robust to moderate violations of the assumptions of independent normal prior distributions, and a replication-based method of estimating standard errors for trait scores provided more accurate and stable results than those originally obtained using the approximated inverse Hessian.

Since the advent of this methodology, organizational research has focused on validating multidimensional pairwise preference assessments in various laboratory and field settings (e.g., Chernyshenko, Stark, Prewett, Gray, Stilson, & Tuttle, 2009; Knapp, & Heffner, 2009; Drasgow,

Stark, Chernyshenko, Nye, Hulin, & White, 2012; Knapp, Heffner, & White, 2011; Stark, Chernyshenko, & Drasgow, 2011), generalizing the psychometric model to more complex item formats and improving methods for estimating MFC item parameters and trait scores (de la Torre, Ponsoda, Leenen, & Hontangas, 2012). Research involving simpler unidimensional models has also sparked speculation that the successful use of subject matter expert ratings of statement extremity for unidimensional pairwise preference test construction and scoring (Stark, Chernyshenko, & Guenole, 2011) can provide a reasonable initial alternative to MFC item parameter estimation, which would dramatically reduce the costs of item pretesting with large samples. Research by Seybert and colleagues has also explored methods for calibrating and scoring unidimensional ideal point single-statement responses using an alternative model to the GGUM – namely Andrich’s Hyperbolic Cosine Model (HCM; Andrich & Luo, 1993) and its variations – with the intent of providing an alternative, more tractable basis for MFC test construction and scoring.

A Thurstonian Model for MFC Data

Maydeu-Olivares and Brown developed a confirmatory factor analytic (CFA) method for collecting and scoring MFC responses in accordance with Thurstone’s (1927) law of comparative judgment (Brown, 2010; Brown & Maydeu-Olivares, 2011, 2013; Maydeu-Olivares, 2001; Maydeu-Olivares & Brown, 2010). For example, when presented with a MFC item tetrad, rather than asking respondents to indicate the statements in each group that are most and least like me, respondents are instructed to rank the statements based on their level of agreement or preference, with 1 being the most preferred and 4 being the least preferred, as shown:

- 2 A. I have almost always completed projects on time.
- 3 B. I have not exercised regularly.
- 1 C. I have enjoyed coordinating the activities of others.
- 4 D. I have a hard time feeling relaxed before an important test.

Assuming transitivity, the ranks are decomposed into a series of dichotomously (0, 1) scored pairwise preference judgments, where the symbol $>$ means “preferred to,” coded 1. In general, for any set of M statements, there are $M(M-1)/2$ unique pairs. For tetrads, there are 6. For the ranks indicated above, the six pairwise preference judgments would be scored dichotomously as shown:

$(A > B)$	$(A > C)$	$(A > D)$	$(B > C)$	$(B > D)$	$(C > D)$
1	0	1	0	1	1

Brown and Maydeu-Olivares (2011) proposed scoring binary responses derived from MFC rank data using a multidimensional normal ogive model, with local dependencies due to statements appearing in the multiple pairs associated with each tetrad having constrained (equal) factor loadings. Brown and Maydeu-Olivares (2013) provided Mplus syntax (Muthén & Muthén, 2010) to compute item loadings, item thresholds and factor scores, which are akin, respectively, to item discrimination, item extremity, and person parameters (trait scores) in traditional IRT terminology. For details on this CFA procedure, readers are encouraged to consult Brown et al. (2011, 2013).

The Thurstonian approach to analyzing MFC rank data has proven effective in a wide range of simulation conditions (Brown & Maydeu-Olivares, 2011). A strong point of this

methodology is that it can be adapted easily for measures involving more or fewer than four alternatives, as well as measures involving mixed formats and multiple groups. In addition, inventories requiring most like me and least like me judgments, such as the AIM, can be seen as providing partial rank data that can be handled by methods designed for missing at random (MAR) responses (Brown & Maydeu-Olivares, 2012, 2013). One minor drawback of this approach is that the underlying item response model is a normal ogive, which assumes a monotonic relationship between factor scores and response propensities. Consequently, statements expressing ambivalence, moderation, or neutrality must be avoided, which reduces the pool available for test construction relative to ideal point models that can accommodate a wider variety of item types (Chernyshenko, Stark, Drasgow, & Roberts, 2007; Roberts, Wedell, & Laughlin, 1999; Stark, Chernyshenko, Williams, & Drasgow, 2006). Another issue that deserves more attention relates to tetrad composition. Research by Maydeu-Olivares and Brown indicates that factor score recovery is influenced by the valences and extremity of the statements composing each tetrad. Specifically, recovery of factor scores is better when tetrads are composed of a mix of positive and negative statements, rather than all positive or all negative, which could have implications for field uses, because tetrads composed of similarly desirable statements may provide greater resistance to faking. However, using four response alternatives that differ somewhat in desirability, as opposed to four, or just two, that are similarly desirable (e.g., Stark, 2002) might improve reactions to testing by allowing examinees to feel they can distance themselves from the most clearly negative descriptors while intrinsically preferring those that are slightly negative.

Summary

The methods described in this chapter represent significant advances in the recent history of MFC testing. The U.S. Army AIM research program (White & Young, 1998) produced a classical test theory method of creating MFC tests that provides scores which can be used for organizational decision making. This work was a springboard for many important research studies (Heggestad, Morrison, Reeve, & McCloy, 2006; McCloy, Heggestad, & Reeve, 2005; Stark, 2002; Stark, Chernyshenko, & Drasgow, 2005) and applications in organizations. The MUPP approach to test construction and scoring (Stark, 2002) described how ipsativity and faking in personality assessment could be addressed with modern psychometric theory. The general model for pairwise preference judgments and the two-stage approach to test construction and scoring laid a foundation for computer adaptive testing (CAT), which significantly reduces testing time while maintaining scoring precision (Stark, Chernyshenko, & Drasgow, 2011; Stark et al., 2012). The Thurstonian model (Brown, 2010; Brown & Maydeu-Olivares, 2011, 2013) provides yet another rigorous and flexible framework for constructing and scoring MFC measures. Although not ideal for CAT, it allows quicker deployment of MFC test forms by eliminating the preliminary statement calibration phase proposed by Stark (2002). It is also readily adapted to different item formats, and it can be implemented easily with widely available statistical software.

Preview of Upcoming Chapters

Chapter 3 discusses more recent advances in modeling MFC tetrad responses from a traditional IRT perspective. It provides a detailed review of de la Torre et al.'s PICK and RANK models, which subsume Stark's (2002) model for pairwise preferences, based on the GGUM. Chapter 4 presents David Andrich's Hyperbolic Cosine Model (HCM; Andrich & Luo, 1993) as

an alternative to the GGUM, which Seybert and colleagues have been exploring as an alternative to the GGUM for noncognitive single-statement responses.

In Chapter 5, a new IRT model for MFC rank order responses that is the focus of this dissertation is introduced. This new model, which is a generalization of the HCM and is henceforth referred to as the Hyperbolic Cosine Model for Multidimensional Rank order responses (HCM-RANK), has several interesting properties that make it an attractive alternative to the GGUM-based PICK and RANK models, which are currently at the forefront of MFC psychometric innovation. Chapter 6 then describes an estimation strategy to obtain parameter estimates using the HCM-RANK.

Chapters 7 through 12 describe simulation studies and results that evaluate the efficacy of MCMC parameter estimation methods developed for scoring HCM-RANK responses. In addition, a study that explores using SME judgments of statement location in place of IRT parameter estimates to expedite test development is described.

CHAPTER 3:

RECENT ADVANCES IN IRT MODELING OF FORCED CHOICE RESPONSES

The previous chapter presented two alternatives to classical test theory methods for analyzing MFC responses. Although the methods differ in several ways, the data used for parameter estimation in both cases stem from explicit or inferred pairwise preference judgments. More specifically, whereas Stark (2002) presented a model designed for explicit pairwise preferences and chose an ideal point model as the basis for parameter estimation, Maydeu-Olivares and Brown proposed a general approach involving ranks. Assuming transitivity, they recode ranks into a set of inferred pairwise preference judgments and estimate parameters via a dominance (normal ogive) model.

An alternative conceptualization of ranks was provided by Luce (1959). Luce viewed ranks as a series of independent preferential choice judgments among sets of successively fewer alternatives. Assigning ranks involves a process, often referred to as *decomposition* (Yellott, 1980, 1997), which holds that when an individual ranks a set of alternatives, he or she makes the first independent preferential choice from the full set, the second independent choice from the remaining set, and so on, until the last rank is determined. This decomposition assumption provides a straightforward alternative way of modeling MFC rank responses, as well as “most like me” and/or “least like me” responses. The probability of a particular set of ranks is just the product of the preferential choice probabilities at each stage of the decomposition. This logic is central to de la Torre et al.’s (2012) PICK and RANK models for MFC item parameter estimation and scoring, which are described below.

The PICK Model for *Most Like* Responses

The PICK model is a generalization of Stark's (2002) MUPP model. It assumes that when a respondent is presented with a set of M alternatives and is asked to make a "most like me" decision, the respondent evaluates each alternative independently until a preference is reached, which implies agreeing with that alternative and disagreeing with all the others. The probability of that *most like* choice is thus the joint probability of that outcome divided by the sum of the probabilities of all possible outcomes. For example, when presented with an item tetrad composed of four statements, A, B, C, and D, the probability of choosing statement A as *most like* is given by:

$$P_{(A>B,C,D)_i}(\theta_{d_A}, \theta_{d_B}, \theta_{d_C}, \theta_{d_D}) = \frac{P\{1,0,0,0\}}{P\{1,0,0,0\}+P\{0,1,0,0\}+P\{0,0,1,0\}+P\{0,0,0,1\}} = \frac{P_A(1)P_B(0)P_C(0)P_D(0)}{P_A(1)P_B(0)P_C(0)P_D(0)+P_A(0)P_B(1)P_C(0)P_D(0)+P_A(0)P_B(0)P_C(1)P_D(0)+P_A(0)P_B(0)P_C(0)P_D(1)}, \quad (3.1)$$

where:

i = the index for each item tetrad, $i = 1$ to I ;

A, B, C, D = the labels for the statements in the item tetrad;

d = the dimension associated with a given statement, where $d = 1, \dots, D$;

$\theta_{d_A}, \dots, \theta_{d_D}$ = the respondent's latent trait scores on the respective dimensions;

$P_A(1), \dots, P_D(1)$ = the probabilities of endorsing statements A through D;

$P_A(0), P_D(0)$ = the probabilities of not endorsing statements A through D; and

$P_{(A>B,C,D)_i}(\theta_{d_A}, \theta_{d_B}, \theta_{d_C}, \theta_{d_D})$ = the probability of a respondent preferring statement A to statements B, C, and D in item tetrad i .

Similarly, letting TOTAL represent the denominator of Equation 3.1 for convenience, the probability of choosing statement B in the tetrad as *most like* is $P\{0,1,0,0\}/TOTAL$. The probability of choosing statement C as *most like* is $P\{0,0,1,0\}/TOTAL$, and the probability of choosing statement D as *most like* is $P\{0,0,0,1\}/TOTAL$.

Importantly, because choosing *most like* is synonymous with expressing a preference, and the logic is the same regardless of the number of alternatives in a set, the PICK model can be used to explain observed ranks for MFC item parameter estimation and scoring and to assign or generate ranks for MFC data simulations. The sections immediately below introduce de la Torre et al.'s RANK model, illustrate how assignment of ranks can be viewed as a sequence of PICK applications, and provide details on how this model can be used to estimate the probabilities of observed ranks, which are needed for MFC tetrad parameter estimation.

The RANK Model for Rank Responses

Following Luce (1959), de la Torre et al. (2012) assume that ranks can be decomposed into a sequence of independent preference, or *most like*, judgments among sets of successively fewer alternatives ($M, M-1, \dots, 2$). At each step in the decomposition process (Critchlow, Flinger, & Verducci, 1991; Yellott, 1997), the PICK model can be used to compute *most like* probabilities, and by the independence assumption, the probability of a set of ranks is therefore just the product of the PICK probabilities.

Continuing with the item tetrad example from above, suppose the four statements composing the tetrad are ranked $A>D>B>C$, where $>$ means preferred. From this set of four, three PICK probabilities are calculated:

1. $P_{(A>B,C,D)}$ = probability of selecting A as *most like* from the set of four;
2. $P_{(D>B,C)}$ = probability of selecting D as *most like* from the remaining three; and

3. $P_{(B>C)}$ = probability of selecting B as *most like* from the remaining two.

The probability of the ranking $A>D>B>C$ is equal to the product of the three PICK probabilities.

Formally, given a respondent's trait scores for the dimensions represented by the statements,

$$P_{(A>D>B>C)}(\theta_{d_A}, \theta_{d_B}, \theta_{d_C}, \theta_{d_D}) = P_{(A>B,C,D)}P_{(D>B,C)}P_{(B>C)} \quad (3.2)$$

The model presented in Equation 3.2 was labeled the RANK model by de la Torre et al. (2012). Although this example illustrates most-to-least ranking, it has been noted that least-to-most preferred ranks could also be assigned, and that might result in different probabilities and selections at each stage (Luce, 1959).

Application of the RANK Model

The RANK model involves a series of PICK applications. Therefore, like the MUPP model (Stark, 2002), a lower-level model is required for computing the underlying statement agreement probabilities. In accordance with Stark (2002) and many recent studies showing good fit of the Generalized Graded Unfolding Model (GGUM; Roberts, Donoghue, & Laughlin, 2000) to single-statement noncognitive responses (Carter & Dalal, 2010; Chernyshenko et al., 2007; Heggstad et al., 2006; Stark et al., 2006; Tay, Drasgow, Rounds, & Williams, 2009), de la Torre et al. (2012) also selected the GGUM as the basis for developing and evaluating item parameter estimation and scoring methods for MFC tetrad responses.

The Generalized Graded Unfolding Model. The GGUM is an ideal point model that can be used for dichotomous and ordered polytomous responses. For PICK applications, the dichotomous version is needed. Specifically, the GGUM is used to compute statement agreement probabilities that underlie *most like* selections. Letting $P(0)$ and $P(1)$ represent the respective

probabilities of disagreeing ($Z=0$) and agreeing ($Z=1$) with a particular statement, given a respondent's latent trait score (θ) on the dimension that statement represents, and three statement parameters (α, δ, τ) reflecting discrimination, location (extremity), and threshold, respectively, we have:

$$P(0) = P(Z = 0|\theta) = \frac{1+\exp(\alpha[3(\theta-\delta)])}{\gamma}, \text{ and} \quad (3.3)$$

$$P(1) = (Z = 1|\theta) = \frac{\exp(\alpha[(\theta-\delta)-\tau])+\exp(\alpha[2(\theta-\delta)-\tau])}{\gamma}, \quad (3.4)$$

where :

$\gamma = 1 + \exp(\alpha[3(\theta - \delta)]) + \exp(\alpha[(\theta - \delta) - \tau]) + \exp(\alpha[2(\theta - \delta) - \tau])$, is a normalizing factor equal to the sum of the numerators of equations 3.3 and 3.4.

Ideal point models, such as the GGUM, assume that a comparison process governs the decision to agree or disagree with a statement. Specifically, they assume a respondent estimates the distance between his or her location and the location of the statement on the underlying trait continuum. If the distance is small the respondent agrees with the statement. If the distance is large the respondent disagrees. Thus, as the perceived distance between the person and the statement increases, the probability of agreeing with the statement decreases. Ideal point models can therefore have *item response functions (IRFs)*, which portray the relationship between trait scores and agreement probabilities, that are nonmonotonic and possibly bell-shaped.

Figure 3.1 presents an example IRF for the dichotomous GGUM for a statement having discrimination, location, and threshold parameters, $\alpha = 1.75$, $\delta = 0.00$, and $\tau = -1.50$, respectively. As in Roberts et al. (2000), the horizontal axis in Figure 1 represents the level of the

underlying latent trait, and the vertical axis shows the probability of agreeing with the statement. It can be seen that the probability of agreement is highest when $(\theta - \delta) = 0$, and it decreases in both directions, resulting in a symmetric, unimodal form. The rate of decrease in the probability of agreement depends on the item discrimination parameter and, to some extent, on the item threshold parameter, while the location parameter determines where the peak of the IRF occurs. (For more details concerning GGUM IRFs, readers may consult Roberts et al., 2000; Roberts & Thompson, 2011; Seybert, Stark, & Chernyshenko, 2013; Stark et al., 2005, 2006).

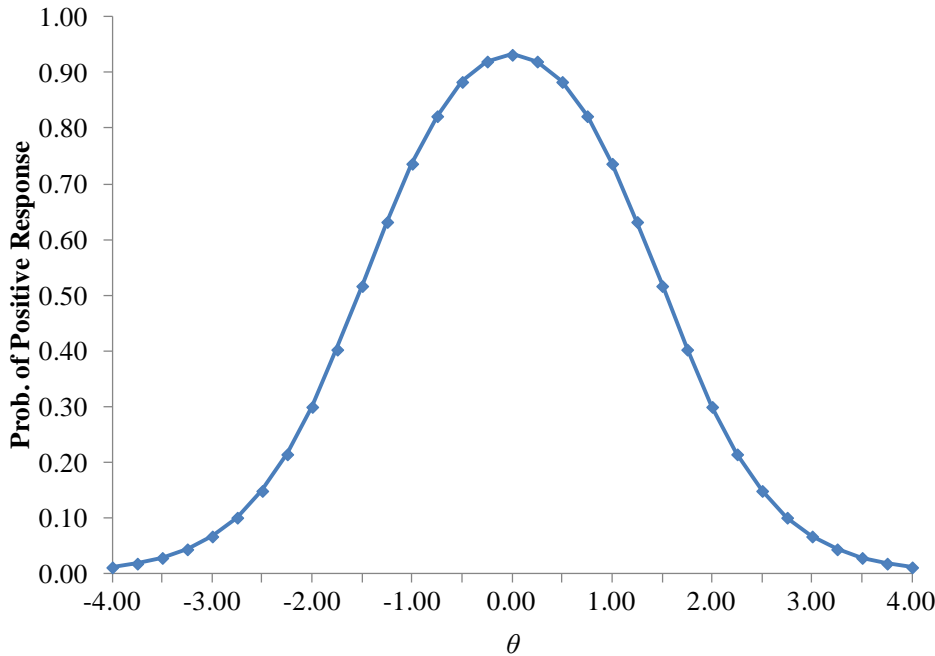


Figure 3.1. Item response function for a two-option GGUM item.

RANK Model Parameter Estimation based on the GGUM. de la Torre et al. (2012) developed and tested Markov chain Monte Carlo (MCMC) parameter estimation methods for MFC tetrad responses using GGUM as the basis for computing PICK *most like* probabilities. They reported accurate recovery of statement locations and trait scores across tests of various

lengths and numbers of dimensions. However, they used extremely tight priors on discrimination and threshold parameters when estimating statement locations; essentially the discrimination and threshold parameters were fixed at 1.00 and -1.00, respectively. Research is needed to determine whether item parameter estimation accuracy can be maintained when these constraints are relaxed and how different test design specifications affect estimation outcomes. It would also be interesting to explore whether relaxing these constraints affects parameter estimation in the absence of any unidimensional items, with and without repeating statements across tetrads. In addition, it remains to be seen whether using an alternative ideal point model as the basis for computing PICK probabilities can improve RANK estimation or streamline MFC test deployment by reducing the sample sizes needed for item calibration.

The next chapter expands on this latter issue by introducing an alternative model as the basis for computing PICK probabilities, namely Andrich's Hyperbolic Cosine Model (HCM; Andrich & Luo, 1993). Stark, Chernyshenko, and Lee (2000) explored the HCM for personality data modeling, but did not pursue it due to estimation difficulties. Since then, Seybert has developed MCMC parameter estimation procedures for the HCM and its variations (Generalized Hyperbolic Cosine Model, Andrich, 1996; Hyperbolic Cosine Model for Pairwise Preferences, HCMPP, Andrich, 1995; Simple HCMPP, Andrich, 1995), which have proven effective in recent simulations (Seybert, Stark, & Chun, manuscript in preparation). Consequently, the HCM provides a viable alternative to the GGUM as a basis for MFC tetrad calibration.

Chapter 4 provides a brief review of Andrich and Luo's (1993) HCM and a special case, called the Simple Hyperbolic Cosine Model (SHCM), which has desirable simplifying features. Chapter 5 then integrates the HCM and SHCM into the PICK and RANK framework to produce

a new, more general model for multidimensional rank order responses, which was explored in three studies.

CHAPTER 4:

THE HYPERBOLIC COSINE MODEL AS AN ALTERNATIVE TO THE GGUM FOR UNIDIMENSIONAL SINGLE-STATEMENT RESPONSES

The MUPP (Stark, 2002; Stark et al., 2005), PICK and RANK (de la Torre et al., 2012) models for MFC responding, described in the previous two chapters, all used the GGUM (Roberts et al., 2000) as the basis for computing the statement agreement probabilities needed for IRT parameter estimation. However, as indicated by those authors, many other models could have been selected for that purpose.

Chernyshenko, Stark, Chan, Drasgow, and Williams (2001) examined the fit of a series of IRT models to personality data for two well-known inventories and found that Levine's (1984) multilinear formula scoring model with ideal point constraints provided excellent fit to data that could not be fitted well by any of the popular dominance models, which assume a monotonic relationship between trait scores and agreement probabilities. Consequently, Stark, Chernyshenko, and Lee (2000) conducted a follow-up study to examine the fit of several ideal point models to those same personality scales. The researchers found that none of the models fit the data well, but they suspected that the problems stemmed from estimation difficulties and, possibly, the lack of model discrimination parameters that would allow IRFs to have a wider variety of shapes. At about the same time, Roberts et al.'s (2000) published their GGUM paper in *Applied Psychological Measurement* and provided the researchers with the GGUM2000 software for another statement calibration study. Stark et al. (2006) examined the fit of the GGUM to personality scales of the *Sixteen Personality Factor Questionnaire 5th Edition* (Cattell

& Cattell, 1995) and found good to excellent fit. Consequently, Stark chose the GGUM as the basis for developing his multidimensional pairwise preference model for noncognitive assessment (Stark, 2002; Stark et al., 2005) and Chernyshenko chose the GGUM for creating ideal point personality measures of the lower-order facets of Conscientiousness (Chernyshenko, 2002; Chernyshenko et al., 2007; Roberts, Chernyshenko, Stark, & Goldberg, 2005).

Since then there has been a stream of research exploring GGUM parameter estimation (Carter & Zickar, 2011a; de la Torre, Stark, Chernyshenko, 2006; Roberts, Donoghue, & Laughlin, 2002; Roberts & Thompson, 2002), differential item functioning detection (Carter & Zickar, 2011b; O'Brien & LaHuis, 2011; Seybert et al., 2013) and suitability for modeling other constructs of interest in organizations, such as job satisfaction (Carter & Dalal, 2010), vocational interests (Tay et al., 2009), and personality (Chernyshenko et al., 2009; O'Brien & LaHuis, 2011; Stark et al., 2006; Weeks & Meijer, 2008). Hence, the GGUM has undoubtedly had a big impact on applied noncognitive measurement – an impact so great, perhaps, that researchers have seemingly halted the search for viable ideal models that began at the start of the last decade. Focusing attention on a particular model is beneficial in terms of accumulating detailed knowledge and systematically addressing questions that will impact practice in the near future. However, limiting attention to one model can create the false impression that other models might not be equally well-suited for organizational applications even when newer and more flexible methods for estimating parameters become available.

Markov chain Monte Carlo (MCMC) methods provide a way to estimate item and person parameters using only the likelihood of a data matrix. Because first and second derivatives are not required, MCMC methods may allow researchers to develop more complex, better fitting models, as well as to advance research with models that have been underutilized because of

estimation difficulties. The Hyperbolic Cosine Model (HCM; Andrich & Luo, 1993) is one such model, and it is a key focus of this dissertation research. The HCM and its variations (Generalized Hyperbolic Cosine Model, Andrich, 1996; Hyperbolic Cosine Model for Pairwise Preferences, HCMPP, Andrich, 1995; Simple HCMPP, Andrich, 1995) were explored for personality measurement applications by Stark, Chernyshenko, and Lee (2000), but not pursued due to questions about the metric of parameter estimates and the fortuitous advent of the GGUM (Roberts et al., 2000).

Given the rising demand for ideal point models in applied assessment and increasing awareness of the capabilities of MCMC estimation, Seybert, et al. (manuscript in preparation) began exploring MCMC parameter estimation for the HCM using the OPENBUGS (Lunn, Spiegelhalter, Thomas & Best, 2009) and Ox (Doornik, 2009) development platforms. Small-scale simulations were conducted which suggested that HCM statement parameters could be estimated accurately with samples much smaller than those typically required for the GGUM (e.g., 400 to 600; de la Torre et al., 2006; Roberts et al., 2002). This finding, in turn, galvanized interest in exploring the HCM as an alternative basis for modeling rank, *most like*, and *least like* responses to MFC tetrads in this dissertation.

The next section provides an overview of Andrich and Luo's (1993) HCM model for single-stimulus responses. Following, I introduce two new models I developed for MFC responses using the HCM as a basis and briefly describe MCMC parameter estimation algorithms that were evaluated by the studies described in succeeding chapters.

The Hyperbolic Cosine Model for Unidimensional Single-Stimulus Responses

Andrich and Luo (1993) developed the HCM for dichotomous unidimensional single-stimulus (i.e., single-statement) responses. The model assumes that a respondent agrees with a

statement when he or she is located close to the statement on the underlying trait continuum (Agrees Closely, AC) and disagrees when he or she is located too far from the statement in either direction. Thus, a respondent can disagree from above (DA) *or* disagree from below (DB). Observed Disagree responses are postulated to result from “folding” or adding these subjective DA and DB response probabilities, and observed Agree responses are proposed to coincide with the Agree Closely probabilities.

To develop their model for observed Disagree ($Z=0$) and Agree ($Z=1$) responses, Andrich and Luo first selected the Rasch model for three ordered categories (Andrich, 1982) as the basis for computing *subjective* response probabilities, coded DB ($X=0$), AC ($X=1$), and DA ($X=2$). Letting θ represent a person parameter (trait score), and letting δ and τ representing statement location and category threshold parameters, respectively, subjective response probabilities were defined as follows:

$$P[DB|\theta] = P[X = 0|\theta] = \frac{1}{1 + \exp(\tau + \theta - \delta) + \exp 2(\theta - \delta)}, \quad (4.1)$$

$$P[AC|\theta] = P[X = 1|\theta] = \frac{\exp(\tau + \theta - \delta)}{1 + \exp(\tau + \theta - \delta) + \exp 2(\theta - \delta)}, \quad (4.2)$$

and

$$P[DA|\theta] = P[X = 2|\theta] = \frac{\exp 2(\theta - \delta)}{1 + \exp(\tau + \theta - \delta) + \exp 2(\theta - \delta)}. \quad (4.3)$$

An illustrative subjective probability plot is presented in Figure 4.1 for a hypothetical statement having $\delta = 0$ and $\tau = 1$. It can be seen that the DB and DA curves are monotonic and s-shaped, like those associated with the Rasch model for dichotomous responses. In contrast, the

AC curve is unimodal and symmetric about δ , with τ indicating the distance from the peak to the intersections of AC with DB and AC with DA. This graph indicates that respondents having traits scores between -1 and +1 are those most likely to Agree Closely with the statement.

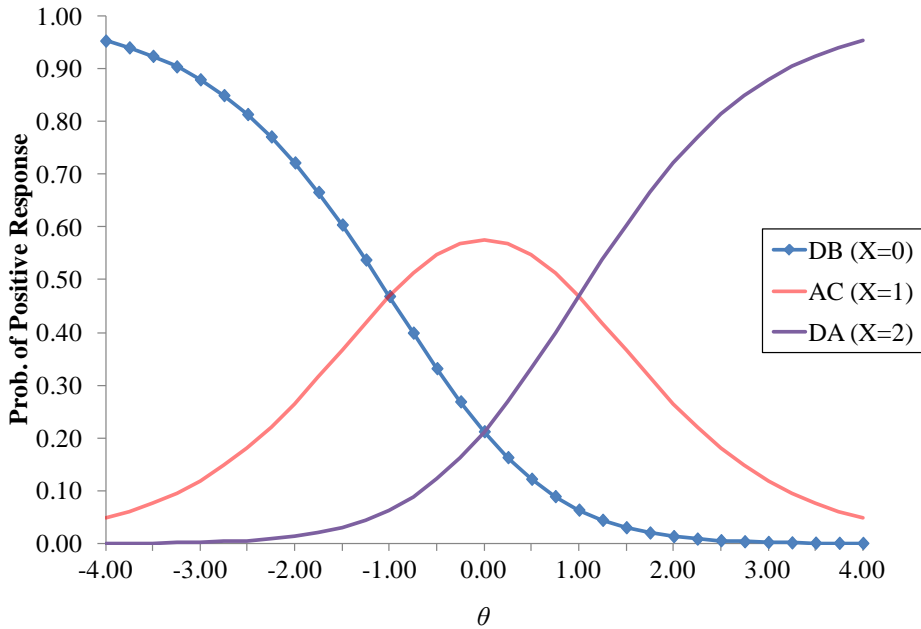


Figure 4.1. Subjective response probability plot.

After choosing a model for subjective response probabilities, Andrich and Luo then defined the probability of an observed Disagree response as $P[Z = 0|\theta] = P[DB|\theta] + P[DA|\theta]$ and the probability of an observed Agree response as $[Z = 1|\theta] = P[AC|\theta]$. After simplification, the following equations, known as the Hyperbolic Cosine Model for single-stimulus binary responses, were obtained:

$$P[Z = 0|\theta] = \frac{2 \cosh(\theta - \delta)}{\exp(\tau) + 2 \cosh(\theta - \delta)}, \quad (4.4)$$

and

$$P[Z = 1|\theta] = \frac{\exp(\tau)}{\exp(\tau) + 2 \cosh(\theta - \delta)}. \quad (4.5)$$

In this form, τ represents a “unit” parameter, referred to as the *latitude of acceptance*, which is somewhat similar to item discrimination parameters in other IRT models (Roberts, Rost, & Macready, 2000). The latitude of acceptance influences both the height and width of the peak of an HCM item response function (IRF), which portrays the probability of agreeing with a statement as a function of trait level (θ). The larger is τ (i.e., the wider is the latitude of acceptance), the more likely a respondent is to agree with a statement regardless of his or her trait level. Figure 4.2 presents three HCM IRFs with $\delta=0$ and varying τ parameters for illustration.

A Special Case: The Simple HCM (SHCM)

Andrich and Luo (1993) discussed several options regarding the estimation of HCM latitude of acceptance parameters. As an alternative to estimating a unique τ for every statement in a measure, a single τ can be estimated by imposing equality constraints across statements, or τ can simply be set to a specific value, as can be done to obtain the Rasch (1960) model from Birnbaum’s (1968) two-parameter logistic model, by setting all discrimination (a) parameters equal to 1.

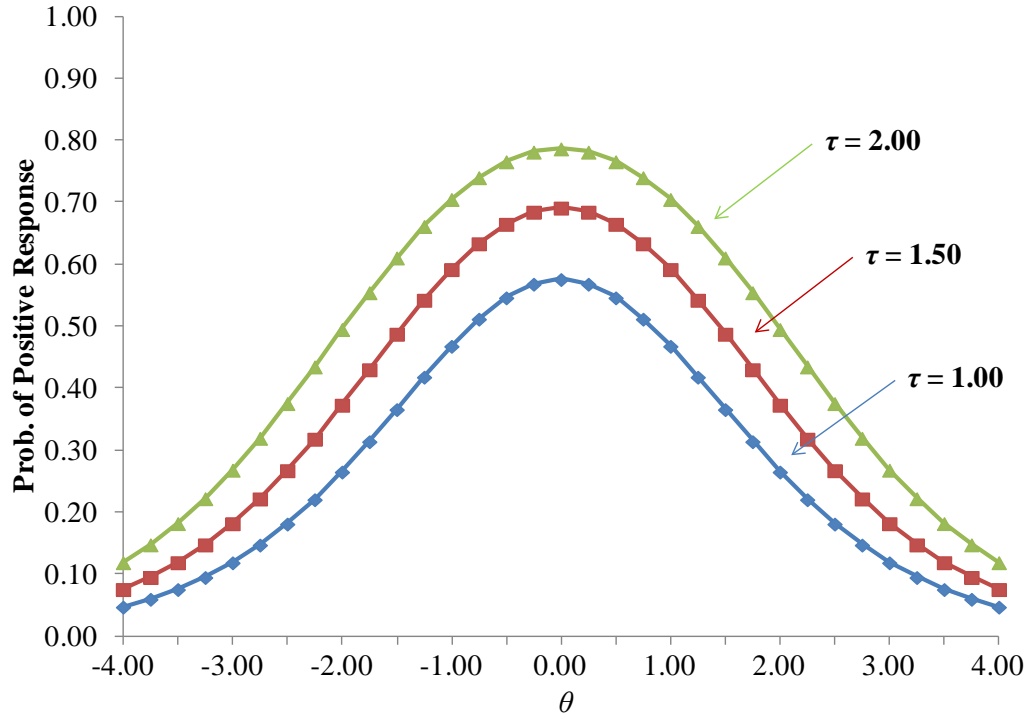


Figure 4.2. HCM item response functions with different latitudes of acceptance.

Because the HCM involves exponential functions, simplification follows from setting τ equal to the natural log of 2 ($\tau = \ln(2)$). Andrich and Luo referred to this special case of the HCM as the Simple HCM, with observed response probability equations shown:

$$P[Z = 0|\theta] = \frac{\cosh(\theta - \delta)}{1 + \cosh(\theta - \delta)}, \quad (4.6)$$

and

$$P[Z = 1|\theta] = \frac{1}{1 + \cosh(\theta - \delta)}. \quad (4.7)$$

Advantages of the HCM and SHCM as a Basis for MFC Test Construction

In comparison with the Generalized Graded Unfolding Model for dichotomous responses (GGUM; Roberts, Donoghue, & Laughlin, 2000), the HCM has a much simpler form and, therefore, provides a more tractable basis for MFC models, such as the MUPP (Stark, 2002; Stark et al., 2005), PICK and RANK (de la Torre et al., 2012) models, discussed in previous chapters. This simplicity becomes more apparent when deriving first and second derivatives of the probability equations, which are needed for computing item information and standard errors, as well as estimating item parameters with marginal maximum likelihood techniques. Moreover, even with MCMC estimation methods that do not require derivatives for parameter estimation, this simplicity may have practical benefits in terms of computing time and the sample sizes required for item calibration.

Other than the few examples provided by Andrich and coauthors when deriving the model and examining parameter recovery with the joint maximum likelihood estimation method implemented in the RUMMFOLD program (Andrich, & Luo, 1996), there have been very few published applications of the HCM and its variations to date. A literature search revealed just two: Touloumtzoglou (1999) who used the model to assess attitudes towards the visual arts, and McGrane (2009) who evaluated measures of ambivalence. As noted by Stark, Chernyshenko, and Lee (2000), who explored the fit of the HCM to personality scales of the Sixteen Personality Factor Questionnaire (5th edition; Cattell & Cattell, 1995), the item parameter estimates provided by RUMMFOLD were on a different scale than the other models. Rather than identifying the metric by assuming the trait distribution has a mean of zero and a variance of 1, as is common

with other IRT software, RUMMFOLD's joint maximum likelihood estimation procedure identifies the metric by constraining location parameters to sum to zero, $\sum_{i=1}^I \hat{\delta}_i = 0$, making it difficult to evaluate fit with external programs that conveniently assume a standard normal trait distribution for fit plots and chi-squares computations (e.g., Drasgow et al., 1995; Stark, 2004; Tay, Ali, Drasgow, & Williams, 2011). This issue is illustrated clearly in Andrich (1996), which reported location parameter estimates ranging from -9.80 to 8.47 for statements reflecting attitudes toward capital punishment.

Summary

In summary, the HCM has several features that make it an attractive alternative to the GGUM (Roberts, Donoghue, & Laughlin, 2000) for single-statement responses, as well as an attractive basis for MFC tetrad applications. However, scaling issues and concerns about the accuracy of joint maximum likelihood parameter estimation with small samples have likely limited its use. Simulation research currently underway by Seybert and colleagues aims to address that issue by providing MCMC estimation algorithms that yield parameter estimates on the familiar standard normal scale. Doing so should facilitate interpretation and evaluations of fit relative to competing models, via programs, such as MODFIT (Stark, 2004). Because this ongoing research has shown that HCM and SHCM parameters can be recovered accurately for samples varying widely in size and tests varying in length, the HCM and SHCM were chosen as the basis for developing new models for MFC PICK and RANK, which are described in upcoming chapters.

CHAPTER 5:
HYPERBOLIC COSINE MODELS FOR MULTIDIMENSIONAL FORCED CHOICE
RESPONSES:
INTRODUCING THE HCM-PICK AND HCM-RANK MODELS

As discussed in Chapter 3, the PICK model provides a general way to compute the probability of a *most like* choice from a set of M alternatives, and the RANK model provides a general way to decompose a set of ranks among M alternatives into a series of $M-1$ independent PICK applications, having probabilities that multiply to give the probability of a particular rank ordering. As a basis for estimating parameters for these models in connection with MFC tetrads, de la Torre et al. (2012) chose the Generalized Graded Unfolding Model (GGUM; Roberts, Donoghue, & Laughlin, 2000) for computing the necessary PICK statement agreement probabilities.

In Chapter 4, it was suggested that Andrich and Luo's (1993) Hyperbolic Cosine Model (HCM) and Simple Hyperbolic Cosine Model (SHCM) provide simpler alternatives to the GGUM for characterizing unidimensional single-statement responses. However, questions concerning the metric of HCM statement parameter estimates and their accuracy in small samples have limited use. It was also stated that ongoing simulation research has shown that newly developed Markov Chain Monte Carlo (MCMC) estimation methods can provide accurate and readily interpretable parameter HCM parameter estimates with samples of various sizes and scales of various lengths (Seybert, Stark, & Chun, manuscript in preparation). Thus, the HCM and SHCM can now be considered viable alternatives for computing PICK statement agreement

probabilities. With this idea in mind, HCM-based versions of the PICK and RANK models and MCMC parameter estimation procedures for MFC were developed. The models and estimation methods are summarized in the following sections of this chapter, with intermediate steps in these derivations provided in Appendix A.

The HCM-PICK: A Hyperbolic Cosine Model for *Most Like* Responses

A Formulation for Tetrads

Following de la Torre et al. (2012), an HCM-based version of the PICK model for tetrads, involving statements A, B, C, and D, can be obtained by substituting the probability expressions for HCM observed disagree ($Z = 0$) and agree ($Z = 1$) responses into the appropriate PICK model terms of Equation 3.1 representing disagreement, $P_A(0)$, $P_B(0)$, $P_C(0)$, and $P_D(0)$, and agreement, $P_A(1)$, $P_B(1)$, $P_C(1)$, and $P_D(1)$, respectively. As shown in Appendix A, HCM-PICK probabilities for *most like* selections from a tetrad are as follows:

$$P_{(A>B,C,D)}_i(\theta_{d_A}, \theta_{d_B}, \theta_{d_C}, \theta_{d_D}) = \frac{T_{ABCD}}{T_{ABCD} + AT_{BCD} + ABT_{CD} + ABCT_D} \quad (5.1a)$$

$$P_{(B>A,C,D)}_i(\theta_{d_A}, \theta_{d_B}, \theta_{d_C}, \theta_{d_D}) = \frac{AT_{BCD}}{T_{ABCD} + AT_{BCD} + ABT_{CD} + ABCT_D} \quad (5.1b)$$

$$P_{(C>A,B,D)}_i(\theta_{d_A}, \theta_{d_B}, \theta_{d_C}, \theta_{d_D}) = \frac{ABT_{CD}}{T_{ABCD} + AT_{BCD} + ABT_{CD} + ABCT_D} \quad (5.1c)$$

$$P_{(D>A,B,C)}_i(\theta_{d_A}, \theta_{d_B}, \theta_{d_C}, \theta_{d_D}) = \frac{ABCT_D}{T_{ABCD} + AT_{BCD} + ABT_{CD} + ABCT_D}, \quad (5.1d)$$

where:

$$\begin{aligned} A &= \cosh(\theta_{d_A} - \delta_A); \\ B &= \cosh(\theta_{d_B} - \delta_B); \end{aligned} \quad (5.1e)$$

$$C = \cosh(\theta_{d_C} - \delta_C);$$

$$D = \cosh(\theta_{d_D} - \delta_D);$$

$$T_A = \exp(\tau_A);$$

$$T_B = \exp(\tau_B);$$

$$T_C = \exp(\tau_C);$$

$$T_D = \exp(\tau_D); \text{ and}$$

where:

i = the index for item tetrads, $i = 1$ to I ;

d = the dimension associated with a given statement, where $d = 1, \dots, D$;

$\theta_{d_A}, \dots, \theta_{d_D}$ = the respondent's latent trait scores on the respective dimensions;

$P_A(1), \dots, P_D(1)$ = the probabilities of agreeing with statements A through D;

$P_A(0), P_D(0)$ = the probabilities of not agreeing with statements A through D;

$P_{(A>B,C,D)_i}(\theta_{d_A}, \theta_{d_B}, \theta_{d_C}, \theta_{d_D})$ = the probability of a respondent preferring statement A to statements B, C, and D in item tetrad I ;

$P_{(B>A,C,D)_i}(\theta_{d_A}, \theta_{d_B}, \theta_{d_C}, \theta_{d_D})$ = the probability of a respondent preferring statement B to statements A, C, and D in item tetrad I ;

$P_{(C>A,B,D)_i}(\theta_{d_A}, \theta_{d_B}, \theta_{d_C}, \theta_{d_D})$ = the probability of a respondent preferring statement C to statements A, B, and D in item tetrad I ;

$P_{(D>A,B,C)_i}(\theta_{d_A}, \theta_{d_B}, \theta_{d_C}, \theta_{d_D})$ = the probability of a respondent preferring statement D to statements A, B, and C in item tetrad I ;

δ = the location of a given statement on the trait continuum; and

τ = a given statement's latitude of acceptance.

The model implies that a respondent will prefer the statement in a tetrad associated with the smallest $(\theta - \delta)$ and the largest latitude of acceptance.

A General Formulation

In the section above, HCM-PICK model was portrayed using notation specific to tetrads, as in de la Torre et al. (2012). However, it can be compactly re-specified for *blocks* of statements involving $M \geq 2$ alternatives, by letting k be an index for statements, ranging from 1 to M . With the necessary substitutions from Equation 5.1e, we obtain the general expression for HCM-PICK probabilities:

$$P_{k|b_i}(\theta_{d_1}, \dots, \theta_{d_M}) = \frac{\exp(\tau_k) \prod_{c \neq k}^M \cosh(\theta_{d_c} - \delta_c)}{\sum_{c=1}^M \left(\exp(\tau_c) \prod_{v \neq c}^M [\cosh(\theta_{d_v} - \delta_v)] \right)}, \quad (5.2)$$

where

i = the index for item blocks involving M statements, where $i = 1$ to I ;

b = the set of statements included in a block;

d = the dimension associated with a given statement, where $d = 1, \dots, D$;

$\theta_{d_1}, \dots, \theta_{d_M}$ = the latent trait values for a respondent on dimensions d_1 to d_M ;

δ = the location parameter for a given statement;

τ = the latitude of acceptance parameter for a given statement; and

$P_{k|b_i}(\theta_{d_1}, \dots, \theta_{d_M})$ = the probability of a respondent selecting statement k as *most like* in the i^{th} block of M statements.

A Special Case: The Simple HCM-PICK (SHCM-PICK)

Andrich and Luo (1993) noted that the HCM latitude of acceptance parameter τ can be estimated for each statement, constrained equal across statements, or set to a particular value. By setting all $\tau = \ln 2$, the expression for the HCM simplified substantially, so they called that special case the Simple HCM (SHCM). Similarly, setting all $\tau = \ln 2$ in Equation 5.2, we obtain the *Simple HCM-PICK*:

$$P_{k|b_i}(\theta_{d_1}, \dots, \theta_{d_M}) = \frac{\prod_{c=1, c \neq k}^M \cosh(\theta_{d_c} - \delta_c)}{\sum_{c=1}^M \left(\prod_{v=1, v \neq c}^M [\cosh(\theta_{d_v} - \delta_v)] \right)}. \quad (5.3)$$

With the SHCM-PICK, most like choices are intuitive because the probabilities depend only on the distance between the person and statement locations. The model predicts that a respondent will choose as *most like* the statement in a block that is closest to him or her on the respective trait continua. Note that this model is essentially a generalization of Andrich's (1995) Simple Hyperbolic Cosine Model for (unidimensional) Pairwise Preferences (Andrich, 1995).

HCM-PICK Response Functions

When items involve more than two dimensions, there is no straightforward way to show *most like* probabilities as a function of trait levels. However, for simpler cases involving just one or two dimensions item response plots and surfaces can be used. Consider, for example, the simplest case of a block involving statements that measure the same dimension. In this case, HCM-PICK probabilities can be plotted like ordinary unidimensional option response functions (ORFs), as shown in Figure 5.1.

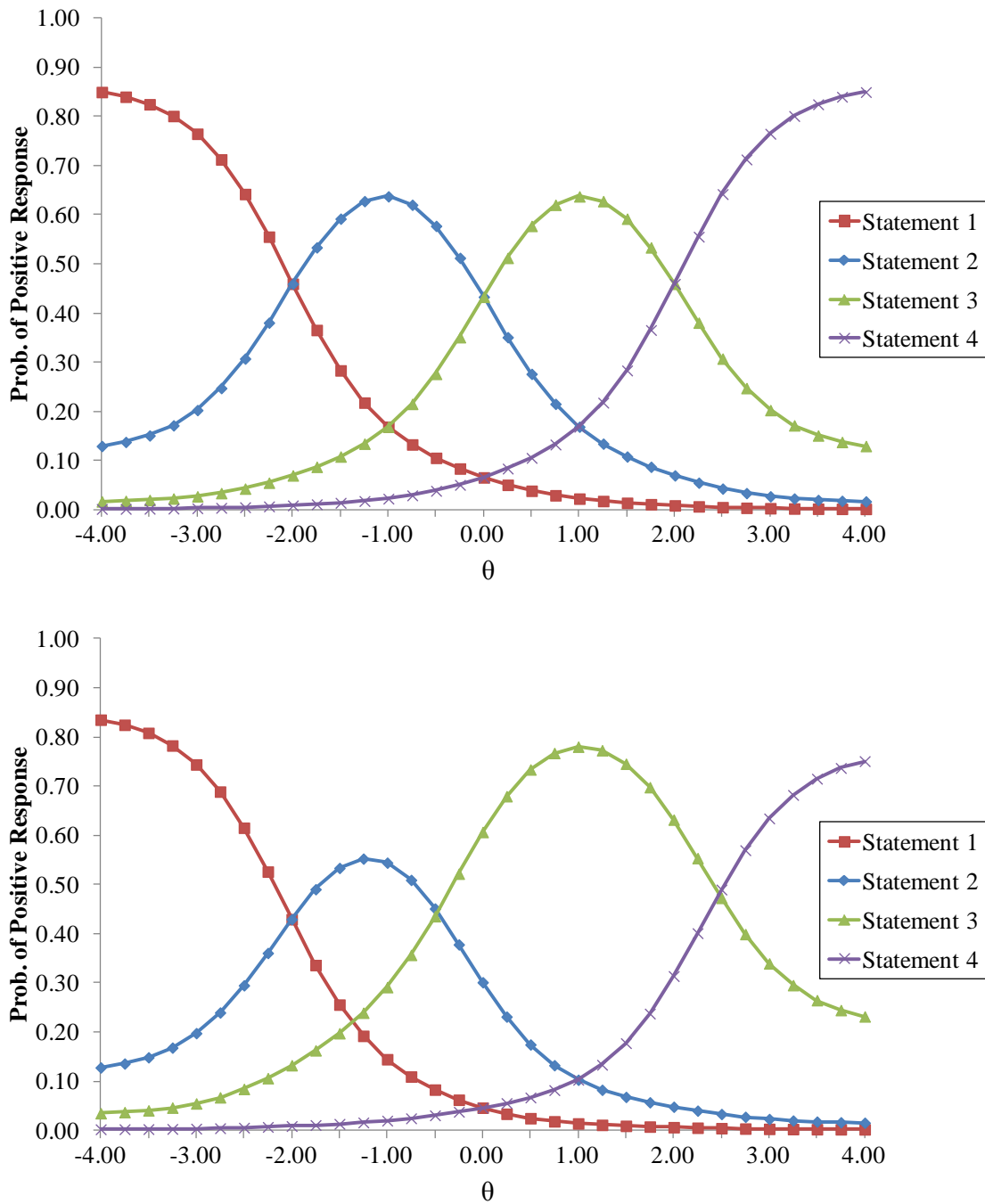


Figure 5.1. HCM-PICK option response functions for a block item involving four statements measuring the same dimension. In both panels, the statements have location parameters of $\delta = -2.00, -1.00, 1.00, 2.00$, respectively. In Panel (a) the statements have the same latitude of acceptance parameter, $\tau = 1.00$. In Panel (b), the latitude of acceptance parameter for Statement 3 was increased to 2.00.

Panel (a) of Figure 5.1 shows HCM-PICK ORFs for a block of four statements having locations parameters of $\delta = -2.00, -1.00, 1.00, 2.00$, respectively, and a common latitude of acceptance ($\tau = 1.00$ for all). It can be seen that the probabilities related to statements 1 and 4 plateau in a negative and positive direction, respectively, as they each are at the extremity of statement locations. That is, because no other statement is closer in relative location to the individuals at such extremes, the probabilities remain flat. For the other statements, as with unidimensional unfolding models for single-statement items, the probability of each statement being selected as *most like* is highest when $\theta = \delta$ and the probability decreases in both directions. However, Panel (b) shows ORFs that would result if the latitude of acceptance for just one statement, #3, were increased to 2.00. This results in a higher and broader peak for Statement 3 and, consequently, lower *most like* probabilities for the other statements in the block, because the probabilities must sum to 1 across statements at every value of θ .

Figure 5.2 presents an HCM-PICK ORF for a pair of statements, A and B, representing *different* dimensions. Statement A has parameters $\delta_A = -1.00, \tau_A = 0.80$ and statement B has parameters $\delta_B = 0.50, \tau_B = 1.50$. The vertical axis represents the probability of preferring statement A to B, given the latent trait values on the horizontal axes corresponding to the dimensions measured by the statements. The response function is a saddle-shaped surface with the probability of selecting statement A being highest along $\theta_{d_A} = \delta_A$ and lowest along $\theta_{d_B} = \delta_B$.

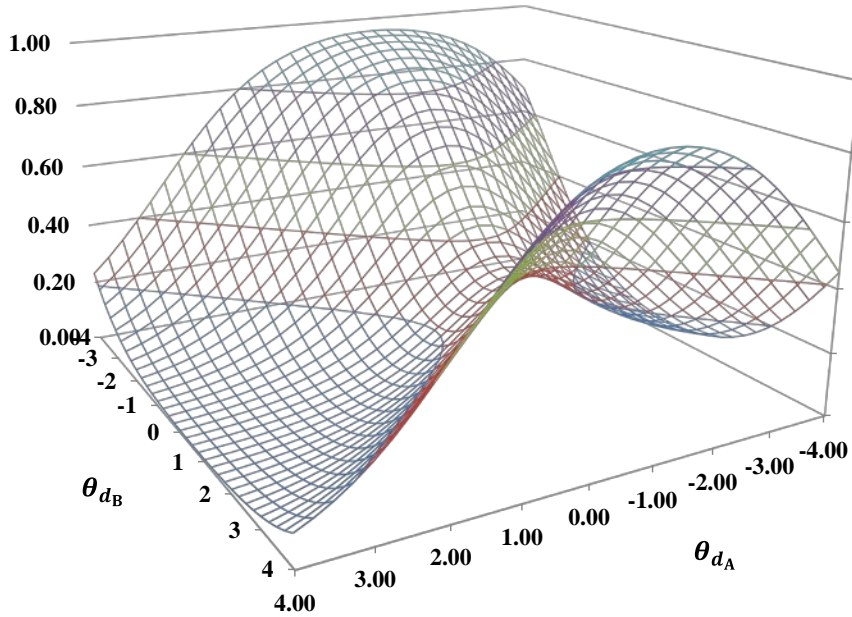


Figure 5.2. HCM-PICK option response function selecting statement A ($\delta = -1.00$, $\tau = 0.80$) over statement B ($\delta = 0.50$, $\tau = 1.50$) in a 2-dimensional pair.

The HCM-RANK: A Hyperbolic Cosine Model for *Rank Order* Responses

de la Torre et al. (2012) showed how one could obtain the probability of rank responses by successive applications of the PICK model, using the GGUM as the basis for computing statement agreement probabilities. The same process can therefore be used to calculate the probability of a set of ranks based on the HCM.

Returning to the Chapter 3 example of an item tetrad for which a respondent indicates the following pattern of preferences, $A > D > C > B$, where $>$ means “preferred,” three HCM-PICK probabilities can be calculated:

1. $P_{(A>B,C,D)}$ = probability of selecting A as *most like* from the block of four statements;
2. $P_{(D>B,C)}$ = probability of selecting D as *most like* from the remaining three; and
3. $P_{(B>C)}$ = probability of selecting B as *most like* from the remaining two.

The probability of the ranking $A>D>B>C$ is equal to the product of the three HCM-PICK probabilities: $P_{(A>D>B>C)_i}(\theta_{d_A}, \theta_{d_B}, \theta_{d_C}, \theta_{d_D}) = P_{(A>B,C,D)}P_{(D>B,C)}P_{(B>C)}$.

To provide a general expression for the probability of rank responses based on successive applications of the HCM-PICK model, as illustrated above, it is convenient to represent a set of ranks as an $(M \times 1)$ column vector $\vec{\mathbf{b}}$, with the rank of the least preferred alternative assigned to row 1, and the rank of the most preferred alternative assigned to row M . For example, the ranking $A>D>B>C$ for the $M=4$, block above would be represented by the column vector

$$\vec{\mathbf{b}}_{M \times 1} = \begin{bmatrix} C \\ B \\ D \\ A \end{bmatrix}. \text{ This organization allows for the derivation of a single expression for the HCM-}$$

RANK, utilizing a product operator to step through successive HCM-PICK probabilities to calculate the probability of a set of ranks. Using this notation, the following general formulation, referred to as the *HCM-RANK* model results:

$$P_{\vec{\mathbf{b}}_i}(\boldsymbol{\theta}) = \prod_{k=2}^M \frac{\exp(\tau_k) \prod_{c=1}^{k-1} \cosh(\theta_{d_c} - \delta_c)}{\sum_{c=1}^k \left(\exp(\tau_c) \prod_{\substack{v=1 \\ v \neq c}}^k [\cosh(\theta_{d_v} - \delta_v)] \right)}, \quad (5.4)$$

where:

i = the index for item blocks involving M statements, where $i = 1$ to I ;

$\vec{\mathbf{b}}_i$ = a vector of assigned ranks for the i^{th} block, arranged from least preferred (1) to most preferred (M);

d = the dimension associated with a given statement, where $d = 1, \dots, D$;

$\boldsymbol{\theta}$ = a vector of latent trait values for a respondent on dimensions d_1 to d_M ;

δ = the location of a statement on the trait continuum;

τ = the latitude of acceptance parameter for a statement; and

$P_{b_i}(\boldsymbol{\theta})$ = the probability of a ranking of M statements by a respondent with trait scores $\boldsymbol{\theta}$.

As was the case with the HCM, setting the latitude of acceptance to $\tau = \ln(2)$ in Equation 5.4, leads to the following simplified model known as the *Simple HCM-PICK* (SHCM-PICK).

$$P_{b_i}(\boldsymbol{\theta}) = \prod_{k=2}^M \frac{\prod_{c=1}^{k-1} \cosh(\theta_{d_c} - \delta_c)}{\sum_{c=1}^k \left(\prod_{\substack{v=1 \\ v \neq c}}^k [\cosh(\theta_{d_v} - \delta_v)] \right)}, \quad (5.5)$$

Summary and Preview

In this chapter, new models were developed to characterize *most like* and rank responses to multidimensional block items. The new HCM-PICK and HCM-RANK models and their special cases, the SHCM-PICK and SHCM-RANK models, provide a basis for constructing and scoring better multidimensional forced choice assessments, such as situational judgment tests (SJTs), which consist of scenarios followed by blocks of statements representing different response styles. In an SJT, examinees are asked to consider each scenario and indicate what they should/would do by choosing the best/most likely option or by ranking options from best/most likely to worst/least likely. The equations for item response functions and item information functions presented above provide the necessary foundations for estimating item and person parameters directly from examinee responses, as well as for improving item quality, building parallel test forms, equating, and detecting differential functioning.

Parameter estimation for the most general model described here, namely the HCM-RANK model, is the focus of upcoming chapters. Chapter 6 provides a brief overview of Markov

chain Monte Carlo (MCMC) estimation and describes an algorithm for estimating HCM-RANK model parameters. Following this, a series of simulation and empirical studies are provided to investigate the efficacy of the HCM-RANK and SHCM-RANK models.

CHAPTER 6:

HCM-RANK Model Item and Person Parameter Estimation

Many methods have been developed and tested for estimating item and person parameters associated with item response theory models. Historically, joint maximum likelihood (JML) and marginal maximum likelihood (MML) methods are among the most popular (Baker & Kim, 2004). In JML estimation, item and person parameters are estimated through a sequential, iterative process, which begins with provisional estimates of item parameters. These provisional item parameters are used to estimate trait scores, which are then used to improve the provisional item parameter estimates, and this back and forth process continues until stable item and person estimates are obtained. The main concern with JML estimation is that item parameter estimates do not necessarily improve with sample size (i.e., they are not consistent), because as sample size increases, so does the number of person parameters that need to be estimated (Hulin, Drasgow, & Parsons, 1983).

Marginal maximum likelihood (MML) estimation methods address this issue by eliminating the dependency of the item parameter estimates on the trait score distribution. In a seminal paper, Bock and Aitkin (1981) illustrated how consistent item parameter estimates could be obtained via an expectation-maximization (EM) algorithm. Person parameter estimates can then be estimated in a separate run using one of many available methods.

An unfortunate drawback of both of JML and MML methods is that estimation involves a maximization process that requires first and second derivatives of a likelihood function with respect to model parameters. Second derivatives, in particular, can become difficult to derive as

model complexity increases. Consequently, methods that do not require explicit expressions for these derivatives have many practical advantages.

Markov chain Monte Carlo (MCMC) methods provide a way to estimate item and person parameters without complicated derivatives (Patz & Junker, 1999a). Instead, MCMC methods estimate model parameters by computing the means and standard deviations of posterior distributions obtained by repeated sampling. Parameters to be estimated are assumed to have prior distributions, which may be chosen on empirical or practical grounds. Provisional parameter values are specified, posterior values are calculated using the likelihood of the response data and the provisional values, and the process is repeated for thousands of cycles. On each cycle, a decision is made to accept or reject a provisional value in favor of a current one, depending on the likelihood of the data under the two alternatives. If a provisional value makes the observed data more likely, then it is accepted; otherwise it is rejected *probabilistically*. The result is a Markov chain, in which the parameter values at any point depend only on the previous cycle. Given enough cycles, this chain theoretically will converge on a stationary distribution that is the desired posterior, regardless of the choice of priors. However, because the early states in the chain clearly depend on the priors, the first few hundred or thousand cycles are typically discarded (i.e., “burn in”) when computing the posterior means and standard deviations that serve as the final item and person parameter estimates.

Note that because MCMC methods estimate item and person parameters simultaneously, it is akin to joint maximum likelihood (JML) estimation, which may raise questions about consistency of the estimates; e.g., do the item parameter estimates improve with sample size? Most research suggests that consistency is not a big concern. But if it is, one solution is to analyze the data twice, treating the item or person parameters as fixed at the values obtained in

the first analysis, and re-estimating the other set. This strategy is akin to the “divide and conquer” approach that is used to estimate item parameters and then trait scores with software that performs marginal maximum likelihood (MML) estimation (Patz & Junker, 1999a).

MCMC Estimation for the HCM-RANK and SHCM-RANK Models

MCMC methods were chosen for estimating HCM-RANK and SHCM-RANK model parameters due to the complexity of the partial derivatives that would be needed for MML estimation. MCMC approaches have been used gainfully with many IRT models (Albert, 1992; Kim & Bolt, 2007; Patz & Junker, 1999a, 1999b), including ideal point models which are increasing in popularity for noncognitive assessment (de la Torre, Stark, & Chernyshenko, 2006; Johnson & Junker, 2003; Roberts & Thompson, 2011). A number of MCMC algorithms have been proposed, with the *Metropolis-Hastings within Gibbs (MH-within Gibbs)* algorithm (Tierney, 1994) being one of the most flexible (for details, see Patz & Junker, 1999a). For that reason the *MH-within Gibbs* method was selected for this research.

The MH-within Gibbs Algorithm

The *MH-within Gibbs* algorithm begins by specifying the likelihood of the response data given the model parameters. Letting I represent block items, $i = 1, 2, \dots, I$, and letting j represent respondents, $j = 1, 2, \dots, N$, the rank-order responses for person j can be written compactly as $\mathbf{X}_j = \{\vec{\mathbf{b}}_{j1}, \vec{\mathbf{b}}_{j2}, \dots, \vec{\mathbf{b}}_{jI}\}'$. The likelihood of the data matrix for N respondents is then given by

$$p(\mathbf{X}|\boldsymbol{\theta}, \boldsymbol{\delta}, \boldsymbol{\tau}) = \prod_j^N \prod_i^I P_{\vec{\mathbf{b}}_{ij}}(\boldsymbol{\theta}_j), \quad (6.1)$$

where $P_{\vec{\mathbf{b}}_{ij}}(\boldsymbol{\theta}_j)$ is the HCM-RANK probability computed using Equation 5.4.

The *MH-within Gibbs* algorithm allows parameters to be updated jointly or individually on each cycle. Because individual updates are convenient for coding as well as for exploring possible estimation problems, individual updates are used in the HCM-RANK model algorithm. All trait scores (θ) are updated first, followed by all statement location (δ) and all latitude of acceptance (τ) parameters, as described below:

- An initial state ($\theta^0, \delta^0, \tau^0$) is set for the parameters in the model. Initial values may be chosen based on prior knowledge or by sampling from carefully chosen prior distributions.
- On each iteration t , the respective model parameters are updated sequentially, as follows:
 1. Proposed (provisional) candidate values, represented as θ^* , for each set of trait scores (e.g., four values drawn for a scale measuring four dimensions), are obtained by sampling from independent normal distributions centered on state $t-1$ with variances chosen to produce acceptance rates near recommended levels (Patz & Junker, 1999a): $\theta^* \sim N(\theta^{t-1}, \sigma^2)$.
 - An acceptance probability for each set of θ^* is computed by dividing the posterior probability of the proposed state by the posterior probability of the current state.
 - If an acceptance probability is greater than 1 (the proposed value is more likely than the $t-1$ value), the proposed set of θ^* is accepted.
 - If an acceptance probability is less than 1, the acceptance probability is compared to a random uniform number. If the acceptance probability exceeds the random uniform number, the proposed set of θ^* is accepted. Otherwise, the value at state $t-1$ is retained.
 - This process is formalized in Equation 6.2:

$$p(\boldsymbol{\theta}^{(t-1)}, \boldsymbol{\theta}^*) = \min \left\{ \frac{P(\mathbf{X} | \boldsymbol{\theta}^*, \delta^{(t-1)}, \tau^{(t-1)}) p(\boldsymbol{\theta}^*)}{P(\mathbf{X} | \boldsymbol{\theta}^{(t-1)}, \delta^{(t-1)}, \tau^{(t-1)}) p(\boldsymbol{\theta}^{(t-1)})}, 1 \right\}. \quad (6.2)$$

2. Proposed candidate values for statement location parameters δ^* are sampled from independent normal distributions centered on state $t-1$ with appropriately chosen variances: $\delta^* \sim N(\delta^{t-1}, \sigma^2)$.
- An acceptance probability for each δ^* is computed by dividing the posterior probability of the proposed state by the posterior probability of the current state.
 - The proposed states are accepted or rejected probabilistically by comparing the acceptance probabilities to random uniform numbers, as shown in Equation 6.3:

$$p(\delta^{(t-1)}, \delta^*) = \min \left\{ \frac{P(\mathbf{X} | \delta^*, \tau^{(t-1)}) p(\delta^*)}{P(\mathbf{X} | \delta^{(t-1)}, \tau^{(t-1)}) p(\delta^{(t-1)})}, 1 \right\}, \quad (6.3)$$

3. Proposed candidate values for latitude of acceptance parameters, τ^* , are sampled from independent normal distributions centered on state $t-1$ with appropriately chosen variances: $\tau^* \sim N(\tau^{t-1}, \sigma^2)$.
- An acceptance probability for each τ^* is computed by dividing the posterior probability of the proposed state by the posterior probability of the current state.
 - The proposed states are accepted or rejected probabilistically by comparing the acceptance probabilities to random uniform numbers, as shown in Equation 6.4:

$$p(\tau^{(t-1)}, \tau^*) = \min \left\{ \frac{P(\mathbf{X}|\theta^t, \delta^t, \tau^*)p(\tau^*)}{P(\mathbf{X}|\theta^t, \delta^t, \tau^{(t-1)})p(\tau^{(t-1)})}, 1 \right\}, \quad (6.4)$$

- This process continues, saving the item and person parameter values on each cycle, until a designated maximum number of cycles is reached. The values obtained before stationarity is believed to occur are typically discarded. Then means, variances, and covariances of the item and person parameters are computed using the remaining cycles to get the desired parameter estimates, standard errors, and covariance information.

Note that to estimate item and person parameters for the SHCM-RANK model, only slight changes to this algorithm are needed. Since the SHCM-RANK model has no latitude of acceptance parameters, Step 3 can be omitted. In addition, if statement location parameters are known in advance, as might be the case when using SME judgments for scoring, location parameters can be fixed on every cycle, leaving just Step 1 to be executed.

These estimation strategies have been implemented in the Ox (Doornik, 2009) programming language to conduct the studies in this dissertation. Effective prior distributions for the θ , δ , and τ parameters were determined at the simulation stage and proposal variances were set for each specific condition following the recommendations laid out by Patz and Junker (1999a).

CHAPTER 7:

STUDY 1: A MONTE CARLO SIMULATION TO ASSESS THE EFFICACY OF HCM-RANK PARAMETER ESTIMATION METHODS

This chapter describes a Monte Carlo study to answer several key questions about HCM-RANK and SHCM-RANK model parameter estimation. First and foremost, the simulation examines the accuracy of MCMC parameter recovery from rank responses, generated under controlled conditions, using statement parameters obtained from real data to increase external validity. Of interest is how closely the parameter estimates obtained *directly from the rank data* match the generating (true) values in each experimental condition, as indicated by correlations between the estimated and true parameters, bias, and root mean square error statistics. This simulation also compares the results of this *direct* estimation process to those obtained through a *two-stage* process involving statement precalibration (Stark, 2002; see Chapter 2). In the two-stage process, statements composing MFC items are administered individually to a sample of respondents and calibrated, one dimension at a time, using a unidimensional model (i.e., *precalibration*). The resulting statement parameter estimates are then used to score the choice or rank responses to the MFC items. Because the direct and two-stage processes have distinct advantages and disadvantages, the findings of this comparison could have important implications for practice.

Study Design

To examine HCM-RANK and SHCM-RANK parameter estimation, 20-item-tetrad MFC tests were constructed and administered to simulated examinees in 16 conditions associated with four fully-crossed independent variables:

- 1) Sample size:
 - a) $N = 250$; and
 - b) $N = 500$.
- 2) Dimensionality of MFC assessment:
 - a) 4 dimensions; and
 - b) 8 dimensions.
- 3) Estimation strategy:
 - a) *Direct*: Estimate item and person parameters directly (simultaneously) from MFC rank responses; and
 - b) *Two-stage*: Precalibrate statements using a unidimensional model; then score MFC rank responses using those statement parameter estimates.
- 4) Model:
 - a) HCM: In *direct* conditions, use the HCM-RANK model to simultaneously estimate item and person parameters from MFC rank responses. In *two-stage* conditions, precalibrate statements using the HCM; then score MFC rank responses via the HCM-RANK; and
 - b) SHCM: In *direct* conditions, use the SHCM-RANK model to simultaneously estimate item and person parameters from MFC rank responses. In *two-stage*

conditions, precalibrate statements using the SHCM; then score MFC rank responses via the SHCM-RANK.

As run times for a single replication for *direct* conditions ranged from 6 to 12 hours, 30 replications were conducted in each condition.

Constructing MFC Measures for the Simulation

Statement Parameter Data

To increase realism, the two MFC tests needed for this simulation were constructed by following procedures used in organizations to develop measures aimed at reducing socially desirable responding. Rather than sampling the generating item parameters and social desirability ratings from idealized distributions for MFC test construction (e.g., Brown & Maydeu-Olivares, 2011; de la Torre et al., 2012), the generating item parameters for this study were obtained by calibrating real single-statement personality data that were collected as part of a larger previous investigation (Loo, manuscript in preparation). A sample of 302 respondents indicated their level of agreement on a 1 (Strongly Disagree) to 4 (Strongly Agree) scale with 160 personality statements (see Appendix B) measuring conscientiousness, emotional stability, openness to experience, and extraversion. These statements were a combination of items obtained from the International Personality Item Pool (IPIP; Goldberg et al., 2006) and others written by two experts familiar with the constructs. To obtain statement parameters, first these data were dichotomized by recoding the Strongly Disagree and Disagree responses as 0s and the Strongly Agree and Agree responses as 1s. Second, HCM (Andrich & Luo, 1993) item parameters were estimated separately for the statements measuring each dimension, using MCMC software developed in an ongoing study by Seybert et al. (manuscript in preparation). Next, model-data fit was examined using fit plots and chi-square statistics (Drasgow et al., 1995) via the MODFIT 4.0

computer program (Stark, 2013). Statements exhibiting poor psychometric properties or poor fit statistics were eliminated from the pool available for MFC test construction.

Finally, the 142 statements surviving this psychometric screening were administered to 75 new respondents using the same four-point scale (1=Strongly Disagree to 4 =Strongly Agree) for the purpose of collecting social desirability ratings. Rather than asking respondents to judge how desirable a statement is (e.g., Heggstad et al., 2006), respondents were simply be asked to answer in a way that presents themselves in a favorable light, as was done in the Assessment of Individual Motivation research by White and Young (1998). The mean score for each statement served as an indicator of its desirability.

Test Design

Tables 7.1 and 7.2 present high-level design specifications for the 4-D and 8-D MFC tests that were used for test construction with this simulation. In each table, column 1 indicates the tetrad number and columns 2 through 5 indicate the dimensions represented by the first, second, third, and fourth statements. As can be seen in Table 7.1, the 4-D test has a simple design. Each tetrad involves a statement representing a different dimension with the first statement always representing dimension 1, the second statement measuring dimension 2, the third statement measuring dimension 3, and the fourth statement measuring dimension 4. For the 8-D MFC test, the number of possible combinations of four dimensions (70) greatly exceeds the desired number of tetrads (20). To address this, a blueprint was designed to balance the number of times dimensions appeared with one another within a tetrad. This led to a diverse grouping of dimensions across tetrads, as can be seen in Table 7.2.

Table 7.1
Dimension Specifications for the 4-D MFC Test

Tetrad	Statement Dimension			
	1	2	3	4
1	1	2	3	4
2	1	2	3	4
3	1	2	3	4
4	1	2	3	4
5	1	2	3	4
6	1	2	3	4
7	1	2	3	4
8	1	2	3	4
9	1	2	3	4
10	1	2	3	4
11	1	2	3	4
12	1	2	3	4
13	1	2	3	4
14	1	2	3	4
15	1	2	3	4
16	1	2	3	4
17	1	2	3	4
18	1	2	3	4
19	1	2	3	4
20	1	2	3	4

Test Assembly

With these design specifications established, the tetrads of the 4-D and 8-D MFC assessments were constructed. To avoid any potential confounds associated with the quality of the statements used to measure conscientiousness, extraversion, agreeableness, and openness to experience, the parameters and social desirability ratings for the statements surviving the psychometric screening were disassociated from their content and pooled. Groups of statements having similar psychometric properties were identified and systematically allocated to meet the dimensionality specifications of the 4-D and 8-D tests in Tables 7.1 and 7.2.

Table 7.2
Dimension Specifications for the 8-D MFC Test

Tetrad	Statement Dimension			
	1	2	3	4
1	1	2	3	4
2	5	6	7	8
3	1	2	5	6
4	3	4	7	8
5	1	5	4	7
6	3	6	2	8
7	3	6	5	1
8	2	8	4	7
9	1	8	2	5
10	3	4	6	7
11	1	3	5	7
12	2	4	6	8
13	1	8	5	4
14	2	3	6	7
15	1	3	7	8
16	2	4	5	6
17	1	2	6	7
18	3	4	5	8
19	1	4	6	8
20	2	3	5	7

For realism, an effort was made to balance the social desirability of the statements within tetrads. For estimation purposes, the amount of information provided by the statements assessing each dimension was balanced; this was accomplished by computing HCM scale information functions for the respective statement sets and exchanging statements as needed to promote congruence.

Test specifications for the 4-D and 8-D tests for HCM-RANK conditions are presented in Tables 7.3 and 7.4, respectively. The total information provided by each dimension, if assessed using a single-stimulus format, is presented in Figures 7.1 and 7.2. In general, statements similar

Table 7.3
Test Specifications for the 4-Dimension Test

Tetrad	Statement	Dimension	Statement Parameters			Tetrad	Statement	Dimension	Statement Parameters		
			δ	τ	SD				δ	τ	SD
1	1	1	-3.50	2.06	0.53	11	41	1	-2.57	3.43	1.46
	2	2	-3.17	1.30	0.55		42	2	-0.43	1.58	1.55
	3	3	-3.41	2.37	0.53		43	3	-0.70	2.41	1.63
	4	4	-3.21	2.09	0.64		44	4	-2.03	3.26	1.63
2	5	1	-3.39	2.52	0.64	12	45	1	2.01	1.75	1.64
	6	2	-1.99	1.19	0.66		46	2	2.51	3.27	1.74
	7	3	-3.14	1.88	0.67		47	3	3.62	2.69	1.76
	8	4	-3.62	2.89	0.70		48	4	-1.12	3.09	1.84
3	9	1	-3.19	2.72	0.73	13	49	1	0.96	2.64	1.90
	10	2	-2.95	1.63	0.73		50	2	2.55	3.15	1.96
	11	3	-3.28	2.34	0.76		51	3	3.18	2.24	1.99
	12	4	-2.53	1.52	0.80		52	4	3.27	3.09	1.99
4	13	1	-3.54	3.17	0.80	14	53	1	1.38	3.08	2.01
	14	2	-2.94	2.37	0.81		54	2	3.22	3.06	2.08
	15	3	-3.07	2.03	0.81		55	3	3.00	2.94	2.08
	16	4	-3.84	2.65	0.81		56	4	2.89	3.30	2.13
5	17	1	-2.89	2.00	0.84	15	57	1	2.77	3.30	2.13
	18	2	-0.90	1.49	0.91		58	2	1.89	3.46	2.15
	19	3	-2.93	2.20	0.88		59	3	2.19	2.80	2.19
	20	4	-2.85	2.17	0.92		60	4	2.56	3.03	2.20
6	21	1	-3.44	3.14	0.92	16	61	1	2.32	3.40	2.20
	22	2	-2.98	3.47	0.97		62	2	2.94	3.43	2.20
	23	3	-3.14	3.44	0.99		63	3	2.41	3.48	2.22
	24	4	-3.22	3.19	1.01		64	4	1.70	2.99	2.26
7	25	1	-1.63	1.62	1.04	17	65	1	2.89	3.33	2.26
	26	2	-2.88	2.51	1.09		66	2	2.71	3.82	2.27
	27	3	-3.02	3.32	1.11		67	3	2.01	3.95	2.28
	28	4	-1.99	2.05	1.13		68	4	2.77	3.11	2.29
8	29	1	-1.26	2.07	1.13	18	69	1	2.08	4.00	2.30
	30	2	-3.05	3.50	1.16		70	2	3.04	3.48	2.33
	31	3	-2.98	3.72	1.16		71	3	0.99	4.06	2.33
	32	4	-0.60	1.70	1.19		72	4	1.43	3.91	2.34
9	33	1	-2.85	3.72	1.19	19	73	1	2.36	3.27	2.34
	34	2	-2.77	3.79	1.21		74	2	1.79	3.73	2.35
	35	3	-0.53	1.41	1.27		75	3	2.29	3.79	2.36
	36	4	1.35	1.46	1.27		76	4	2.13	4.06	2.36
10	37	1	-0.68	2.09	1.28	20	77	1	0.27	3.92	2.39
	38	2	-1.54	2.63	1.36		78	2	2.45	3.64	2.37
	39	3	-2.26	3.26	1.39		79	3	2.58	3.96	2.37
	40	4	-0.24	1.86	1.41		80	4	1.84	3.81	2.40

Table 7.4
Test Specifications for the 8-Dimension Test

Tetrad	Statement	Dimension	Statement Parameters			Tetrad	Statement	Dimension	Statement Parameters		
			δ	τ	SD				δ	τ	SD
1	1	1	-3.78	1.44	0.47	11	41	1	-0.24	1.86	1.41
	2	2	-3.50	2.06	0.53		42	3	-2.57	3.43	1.46
	3	3	-3.17	1.30	0.55		43	5	-2.40	4.01	1.53
	4	4	-3.70	1.58	0.59		44	7	-0.43	1.58	1.55
2	5	5	-3.23	1.42	0.62	12	45	2	-0.70	2.41	1.63
	6	6	-3.39	2.52	0.64		46	4	-2.25	4.05	1.66
	7	7	-1.99	1.19	0.66		47	6	2.51	3.27	1.74
	8	8	-3.14	1.88	0.67		48	8	3.62	2.69	1.76
3	9	1	-3.54	2.22	0.67	13	49	1	0.11	2.95	1.77
	10	2	-3.19	2.72	0.73		50	8	0.96	2.64	1.90
	11	5	-2.95	1.63	0.73		51	5	2.55	3.15	1.96
	12	6	-3.28	2.34	0.76		52	4	0.60	2.77	1.92
4	13	3	-3.19	1.75	0.79	14	53	2	3.28	3.12	2.05
	14	4	-3.54	3.17	0.80		54	3	1.38	3.08	2.01
	15	7	-2.94	2.37	0.81		55	6	3.22	3.06	2.08
	16	8	-3.84	2.65	0.81		56	7	3.00	2.94	2.08
5	17	1	-2.94	1.90	0.81	15	57	1	2.57	2.92	2.11
	18	5	-2.89	2.00	0.84		58	3	2.77	3.30	2.13
	19	4	-1.55	1.54	0.85		59	7	1.89	3.46	2.15
	20	7	-2.93	2.20	0.88		60	8	2.19	2.80	2.19
6	21	3	-0.90	1.49	0.91	16	61	2	2.90	3.32	2.19
	22	6	-3.44	3.14	0.92		62	4	2.56	3.03	2.20
	23	2	-3.01	2.81	0.97		63	5	2.94	3.43	2.20
	24	8	-3.14	3.44	0.99		64	6	2.41	3.48	2.22
7	25	3	-2.80	3.31	0.99	17	65	1	3.15	3.39	2.24
	26	6	-1.63	1.62	1.04		66	2	2.89	3.33	2.26
	27	5	-2.88	2.51	1.09		67	6	2.71	3.82	2.27
	28	1	-2.06	1.86	1.09		68	7	2.01	3.95	2.28
8	29	2	-1.99	2.05	1.13	18	69	3	2.44	3.35	2.29
	30	8	-1.26	2.07	1.13		70	4	2.08	4.00	2.30
	31	4	-3.05	3.50	1.16		71	5	3.04	3.48	2.33
	32	7	-1.46	1.54	1.17		72	8	0.99	4.06	2.33
9	33	1	-1.62	2.24	1.17	19	73	1	1.69	2.67	2.34
	34	8	-2.85	3.72	1.19		74	4	2.36	3.27	2.34
	35	2	-2.77	3.79	1.21		75	6	1.79	3.73	2.35
	36	5	-0.53	1.41	1.27		76	8	2.29	3.79	2.36
10	37	3	1.35	1.46	1.27	20	77	2	2.24	3.79	2.36
	38	4	1.46	1.60	1.35		78	3	2.78	3.24	2.37
	39	6	-1.54	2.63	1.36		79	5	0.27	3.92	2.39
	40	7	-2.26	3.26	1.39		80	7	2.58	3.96	2.37

in social desirability tended to have similar locations, but a few tetrads exhibited more variety. For example, Tetrad 11 in both the 4-D and 8-D tests contains two negatively located statements and two relatively central statements. Note that in the SHCM-RANK conditions, the test specifications were modified so that each τ parameter was set equal to $\ln(2)$.

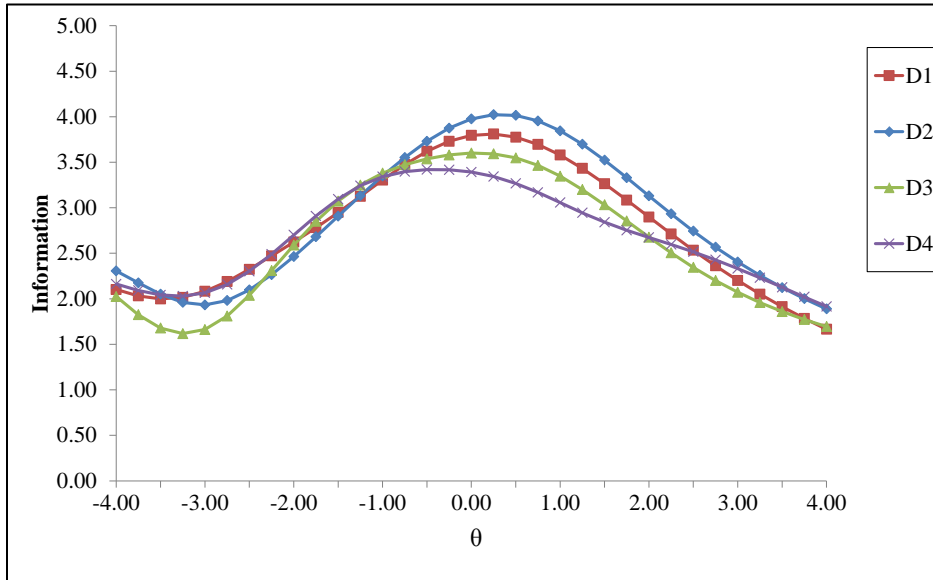


Figure 7.1. Test information functions for each dimension in the 4-D test conditions.

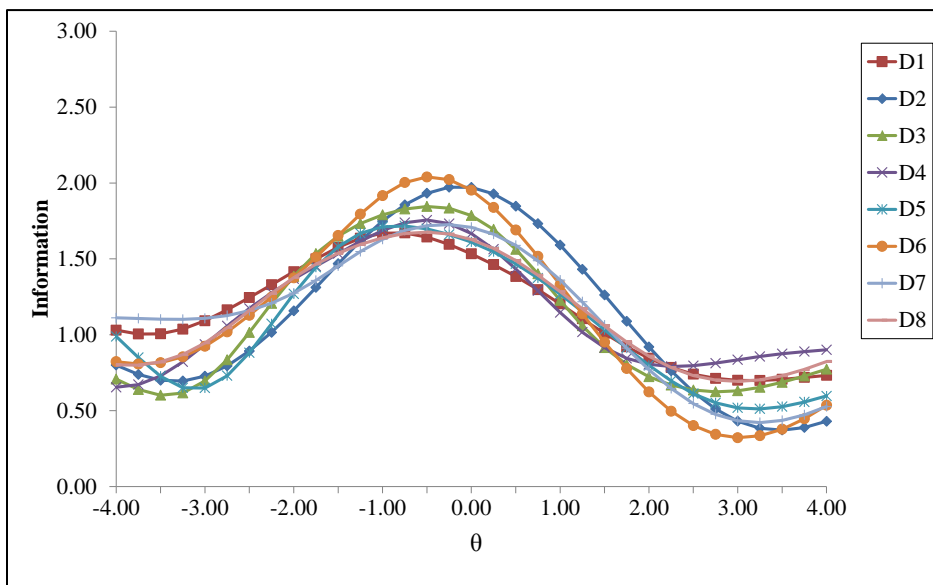


Figure 7.2. Test information functions for each dimension in the 8-D test conditions.

Simulation Details

Generating Rank Responses for MFC Tetrads

HCM-RANK and SHCM-RANK response data were generated as follows:

1. For the designated number of respondents and dimensions measured in each experimental condition, trait scores were sampled randomly from independent standard normal distributions. These trait scores are referred to henceforth as the “generating,” “known,” or “true” trait scores.
2. For each MFC tetrad, the true trait scores and the true statement parameters were used to compute HCM-PICK (Equation 5.1) or SHCM-PICK (Equation 5.2) probabilities. These probabilities were used to divide a 0 to 1 probability interval into four segments, each corresponding to a statement. A random uniform number was generated, the segment into which the number fell was identified, and the corresponding statement was designated as *most like*. That statement was designated as the highest ranked.
3. The PICK probabilities for the three remaining alternatives in the tetrad were recomputed. A 0 to 1 probability interval was divided into three segments using those values. A new random uniform number was generated, the segment into which the number fell was identified, and the corresponding statement was designated as *most like*. That statement was designated as the second-highest ranked.
4. The PICK probabilities for the two remaining alternatives in the tetrad were recomputed. A 0 to 1 probability interval was divided into two segments using those values. A new random uniform number was generated, the segment into which the number fell was identified, and the corresponding statement was designated as *most like*. That statement was designated as the third-highest ranked.

5. The remaining statement in the tetrad was designated as lowest ranked.

Generating Single-Statement Responses for Statement Precalibration in Two-Stage

Conditions

1. For the designated number of respondents and dimensions measured in each experimental condition, trait scores were sampled randomly from independent standard normal distributions. These trait scores are referred to henceforth as the “generating,” “known,” or “true” trait scores.
2. For the statements measuring each dimension, the true trait scores and the true statement parameters were used to compute HCM (Equation 4.5) or SHCM agreement (Equation 4.7) probabilities. These probabilities were compared to randomly generated uniform numbers. In each case, if the probability exceeded the random number, then the response was coded as 1 (agree); otherwise the response was coded as 0 (disagree).

Simulation Process in *Direct* Conditions

In *Direct* conditions, item and person parameters were estimated directly from the generated rank responses. Data generation and parameter estimation proceeded as follows:

1. HCM-RANK and SHCM-RANK responses were generated for samples of 250 and 500 respondents using the 4-D and 8-D MFC tetrad tests described above.
2. Item and person parameters were estimated directly from the rank responses, using the MCMC algorithms developed for this dissertation, and the results were saved.
3. Steps 1 and 2 were repeated until 30 replications were performed. Then indices of estimation accuracy were computed.

Simulation Process in *Two-Stage* Conditions

In *Two-Stage* conditions, person parameters were estimated from tetrad rank responses using precalibrated statement parameters. Data generation and parameter estimation proceeded as follows:

1. *Precalibration*: Single-statement dichotomous responses were generated, one dimension at a time, for samples of 250 and 500 respondents using true parameters for the statements included in the 4-D and 8-D MFC tetrad tests. These dichotomous responses were then calibrated using the HCM or SHCM to obtain statement parameter estimates used for scoring “future samples” of MFC tetrad rank responses.
2. *MFC test administration and scoring*: HCM-RANK or SHCM-RANK responses were generated for new samples of 250 and 500 respondents, for the 4-D and 8-D MFC tetrad tests, using the true statement parameters. The rank response data were then scored with the HCM-RANK or SHCM-RANK MCMC algorithm using the statement parameter estimates from the precalibration phase. To examine the upper-bound of trait recovery, responses were also scored using the true statement parameters.
3. Steps 1 and 2 were repeated until 30 replications were performed. Indices of estimation accuracy were then computed.

Indices of Estimation Accuracy

Estimation accuracy was evaluated using three indices. First, Pearson correlations were computed between the estimated and true item and person parameters averaged over replications. Correlations above .9 are generally considered good to excellent in parameter recovery studies.

To provide another overall indication of parameter recovery for each condition, an average root mean square error statistic (RMSE) was computed for the item and person parameters as follows:

$$\text{RMSE}(\hat{\delta}) = \sqrt{\frac{\sum_{r=1}^R \sum_{s=1}^S (\hat{\delta}_{rs} - \delta_s)^2}{R*S}}, \quad (7.1)$$

$$\text{RMSE}(\hat{\tau}) = \sqrt{\frac{\sum_{r=1}^R \sum_{s=1}^S (\hat{\tau}_{rs} - \tau_s)^2}{R*S}}, \text{ and} \quad (7.2)$$

$$\text{RMSE}(\hat{\theta}) = \sqrt{\frac{\sum_{d=1}^D \sum_{r=1}^R \sum_{j=1}^N (\hat{\theta}_{rj} - \theta_j)^2}{R*N*D}}, \quad (7.3)$$

where:

r = the index for replications, 1 to R;

s = the index for statements, 1 to S;

j = the index for respondents, 1 to N;

d = the index for dimensions, 1 to D;

δ_s = the true location parameter for statement s ;

$\hat{\delta}_{rs}$ = the estimated location parameter for statement s on replication r ;

τ_s = the true latitude of acceptance parameter for statement s ;

$\hat{\tau}_{rs}$ = the estimated latitude of acceptance parameter for statement s on replication r ;

θ_j = the true trait score for respondent j ; and

$\hat{\theta}_{rj}$ = the estimated trait score for respondent j on replication r .

Finally, to provide information about parameter recovery for individual statements which might be helpful when choosing priors for MCMC estimation, the average statement parameter estimate across replications was computed and a scatter-plot of the generating and average estimates was examined.

MCMC Estimation Prior Distributions and Initial Parameter Values

For MCMC statement precalibration with the HCM in *two-stage* conditions, prior distributions and starting values were chosen in accordance with Seybert et al. (manuscript in preparation). Specifically, a bisection method, adapted from Roberts and Laughlin (1996), was used to obtain starting values for statement location (δ) and latitude of acceptance (τ) parameters. Starting values for person parameters (θ) were set at 0. For location parameters, normal priors with means equal to the starting values and variances equal to 1 were chosen. For latitude of acceptance parameters, four-parameter beta priors with support $(-2, 5)$ and shape parameters $(4, 3.5)$ were used. The prior distribution for person parameters was standard normal.

In *direct* estimation conditions with the HCM-RANK model, starting values and prior distributions were based on research with the HCM and several pilot simulations. Independent standard normal priors were chosen for person parameters (θ). Location parameters (δ) utilized a weak four-parameter beta prior with support parameters $(-5, 5)$ and shape parameters $(2, 2)$. And latitude of acceptance parameters (τ) utilized a four-parameter beta prior with support $(-1, 5)$ and shape parameters $(4, 3.5)$. All person parameters were assigned starting values (θ^0) of 0. All latitude of acceptance parameters were assigned starting values (τ^0) of 2. Location parameters were assigned starting values (δ^0) of -3, 0, or +3, under the assumption that SMEs are able to provide rough estimates of statement extremity. For simulation purposes, if the true location parameter was below -1.00, a starting value of -3 was assigned. If the true location parameter

was between -1.00 and +1.00, a value of 0 was assigned. And if the true location parameter was greater than 1.00, a starting value of 3 was assigned.

MCMC Estimation Burn-In and Chain Length

Two important considerations in MCMC estimation are the number of iterations needed for chains to converge and the number of iterations following convergence from which inferences about model parameters can be drawn. The sum of these numbers determines the maximum number of iterations to run when estimating model parameters.

Convergence means that a chain has reached a stationary state so that samples are being drawn from the desired posterior distributions. Since current states no longer depend on initial states after convergence, the original choices of starting values and priors become irrelevant. The iterations preceding convergence are commonly referred to as “burn-in” samples and are typically discarded. “Post-burn-in” samples are used to compute means and standard deviations of the posterior draws that represent the desired parameter estimates and standard errors, respectively.

Several methods have been proposed for checking convergence and determining the necessary numbers of burn-in and post-burn-in iterations. Simultaneously running multiple chains starting with different initial states and examining the agreement after a designated number of iterations has proven to be practical and effective (Patz & Junker, 1999a). In a review of MCMC estimation for IRT models, Wollack, Bolt, Cohen, and Lee (2002) found that the majority of studies utilized burn-in samples of 300 to 5,000 iterations. The number of post burn-in samples frequently ranges from one-tenth to three-times as many iterations as used for burn-in.

In preparation for this study, pilot simulations were conducted using three simultaneous chains. For HCM-RANK *direct* estimation, it was found that convergence occurred at approximately 20,000 iterations. For *two-stage* estimation, 20,000 iterations were also needed for convergence during HCM statement precalibration, but only 2,000 were needed for subsequent HCM-RANK scoring.

In this study, to insure that convergence occurred on every replication in every condition, substantially more than the necessary numbers of burn-in and post-burn-in iterations were performed. However, only one chain was run due to extremely long runtimes. In *direct* estimation conditions, 100,000 total iterations were performed, and the first 50,000 were discarded. The same specifications were used for HCM statement precalibration in the *two-stage* estimation conditions. For HCM-RANK scoring in the *two-stage* conditions, 20,000 total iterations were performed and 5,000 were discarded as burn-in.

Hypotheses

Due to a lack of studies examining the recovery of item and person parameters directly from rank-order response data, experience with single-statement estimation was used to formulate the following hypotheses.

1. Parameters will be estimated more accurately in the large sample (N=500) conditions than in the small sample (N=250) conditions, as indicated by significantly larger Pearson correlations between estimated and true parameters and significantly lower RMSE statistics.
2. Parameters will be estimated more accurately (indicated by significantly larger Pearson correlations between estimated and true parameters and significantly lower RMSE

statistics) with 4-D tests than with 8-D tests, because keeping test length constant (20 items) means that each dimension in the 8-D test is represented by fewer statements.

3. No significant differences will be found for person parameter recovery from rank responses in the *direct* and *two-stage* estimation conditions.
4. No significant differences will be found for person parameter recovery in the HCM and SHCM conditions.
5. Significant differences will be found for statement recovery in the *direct* and *two-stage* estimation conditions.
6. In HCM conditions, statement location parameters will be estimated more accurately than latitude of acceptance parameters, as indicated by significantly larger Pearson correlations between estimated and true parameters and significantly lower RMSE statistics.

Hypotheses were tested using MANOVA and the visual inspection of plots of statement bias.

Eta squared effect sizes were obtained to evaluate the overall influences of the independent variables on study results.

CHAPTER 8: STUDY 1 RESULTS

The purpose of this study was to examine the accuracy of HCM-RANK and SHCM-RANK statement and person parameter recovery through a Monte Carlo simulation. The recovery of parameters was examined by constructing MFC item tetrads according to the design specifications detailed in Chapter 7. Following that, a *direct* estimation or *two-stage* estimation process was used to generate and estimate response data and results were averaged over replications and then compared to the generating values to obtain indices of estimation accuracy.

Simulation Results

Table 8.1 shows the overall statement parameter recovery statistics for each condition, averaged across replications and the individual statements. The top portion of the table shows the average correlations between the generating and estimated parameters, and the bottom portion shows the root mean square error (RMSE) statistics. (Note that only HCM-RANK results are shown for τ because the values were fixed at $\ln(2)$ for the SHCM-RANK estimation.) Overall, it appears that statement location parameters (δ) were relatively well estimated, with correlations above .95 in all cases and RMSEs as low as .161. Latitude of acceptance parameters, however, were not as well estimated, with correlations ranging from .505 to .831, and RMSEs only as low as .454. Location parameter estimates also had markedly smaller RMSEs in the SHCM-RANK conditions than in the HCM-RANK conditions. As was expected, parameter estimates were generally better with samples of 500 than 250, and with 4-D tests than 8-D tests. Finally, for the

HCM-RANK the *direct* estimation conditions showed larger correlations and smaller RMSEs than the *two-stage* estimation conditions, but the opposite was the case for the SHCM-RANK.

Table 8.1
Statement Parameter Recovery Statistics for Each of the Experimental Conditions

Recovery Statistic	Number of Dimensions: Parameter	Model	Estimation Strategy							
			Two-Stage				Direct			
			4		8		4		8	
			N = 250	N = 500	N = 250	N = 500	N = 250	N = 500	N = 250	N = 500
Correlation	δ	SHCM-RANK	0.996	0.998	0.995	0.998	0.993	0.995	0.990	0.995
		HCM-RANK	0.976	0.982	0.968	0.975	0.984	0.987	0.981	0.986
	τ	HCM-RANK	0.781	0.831	0.734	0.785	0.504	0.511	0.504	0.554
RMSE	δ	SHCM-RANK	0.231	0.161	0.249	0.171	0.321	0.262	0.370	0.282
		HCM-RANK	0.587	0.500	0.677	0.594	0.478	0.433	0.528	0.443
	τ	HCM-RANK	0.510	0.454	0.595	0.538	0.927	0.935	0.898	0.878

Note. RMSE = average root mean square error.

Moving next to person parameter (θ) recovery, Table 8.2 presents the correlations between generating and estimated trait scores and the RMSE values, averaged across dimensions and persons. Overall, the correlations between generating and estimated trait scores were nearly identical for *two-stage* and *direct* estimation and very similar for 4-D and 8-D tests, regardless of sample size. The correlations were also remarkably similar for the SHCM-RANK and HCM-RANK models, although the HCM-RANK RMSEs were notably smaller, perhaps because items were more informative due to variation in the latitude of acceptance parameters. This is intriguing given the large RMSEs for τ in Table 8.1. It suggests that trait score recovery is largely driven by location parameters and, consistent with a recent study by Stark, Chernyshenko, and Guenole (2011), trait estimation is fairly robust to error in statement parameter estimates.

Table 8.2
Person Parameter Recovery Statistics for Each of the Experimental Conditions via Rank Responses

Recovery Statistic		Estimation Strategy							
		Two-Stage				Direct			
		Number of Dimensions: 4		8		4		8	
Model	N = 250	N = 500	N = 250	N = 500	N = 250	N = 500	N = 250	N = 500	
Correlation	SHCM-RANK	0.878	0.882	0.840	0.839	0.882	0.884	0.840	0.842
	HCM-RANK	0.876	0.879	0.831	0.836	0.880	0.881	0.837	0.838
RMSE	SHCM-RANK	0.629	0.621	0.675	0.677	0.499	0.499	0.562	0.565
	HCM-RANK	0.482	0.472	0.548	0.546	0.476	0.470	0.545	0.542

Note. RMSE = average root mean square error.

Because the first part of *two-stage* HCM-RANK and SHCM-RANK estimation involved statement precalibration using dichotomous unidimensional responses, statement parameter estimates were also available to compute trait scores based on the unidimensional SHCM and HCM models. Table 8.3 shows the RMSEs and correlations of those estimates with the generating parameters. Note that trait scores for 4-D and 8-D tests were based on 20 and 10 statements, respectively, so better estimation was expected with 4-D tests.

As can be seen in Table 8.3, despite the correspondence between the models used to generate, calibrate, and score the data in this scenario, the correlations between the generating and estimated trait scores are actually slightly lower, and the RMSEs are larger, than the values in the corresponding SHCM-RANK and HCM-RANK conditions in Table 8.2. This suggests that despite the greater complexity of the MFC format and scoring methods, rank responses are more informative than Agree/Disagree responses to individual statements. In future research it would be interesting to see whether MFC methods outperform unidimensional polytomous scoring and how item and test information functions compare.

Table 8.3

Person Parameter Recovery Statistics for Each of the Experimental Conditions via Single-Statement Responses

Recovery Statistic	Model	Number of Dimensions			
		4		8	
		N = 250	N = 500	N = 250	N = 500
Correlation	SHCM	0.796	0.792	0.669	0.672
	HCM	0.862	0.865	0.769	0.767
RMSE	SHCM	0.608	0.609	0.742	0.741
	HCM	0.508	0.504	0.641	0.643

Note. RMSE = average root mean square error.

To better understand how well individual statement parameters were recovered, Figures 8.1, 8.2, and 8.3 plot the average estimated statement location and latitude of acceptance parameters (vertical axis) versus the generating parameters (horizontal axis) in each condition. The diagonal line represents perfect estimation. Comparing the left panels of Figures 8.1 and 8.2, it can be seen that δ parameters were generally closer to the generating values in the *direct* estimation conditions, although both the *direct* and *two-stage* methods performed very well. In contrast, the right panels of Figures 8.1 and 8.2 indicate that τ parameters were not nearly as well estimated and, surprisingly, τ parameters were more accurately recovered in the *two-stage* conditions. Looking more closely at the *direct* estimation plots, the τ parameters appear to be regressed toward the mean of the prior distribution, 2.30, suggesting that a weaker prior or alternative prior distribution should be considered in future studies.

Figure 8.3 shows δ parameter recovery plots for 4-D and 8-D tests in the SHCM-RANK conditions. Clearly, SHCM-RANK δ recovery was far better than HCM-RANK recovery with both estimation methods. In addition, it can be seen that parameter recovery was excellent across the trait range in *two-stage* conditions, but in *direct* conditions larger biases were observed near the extremes.

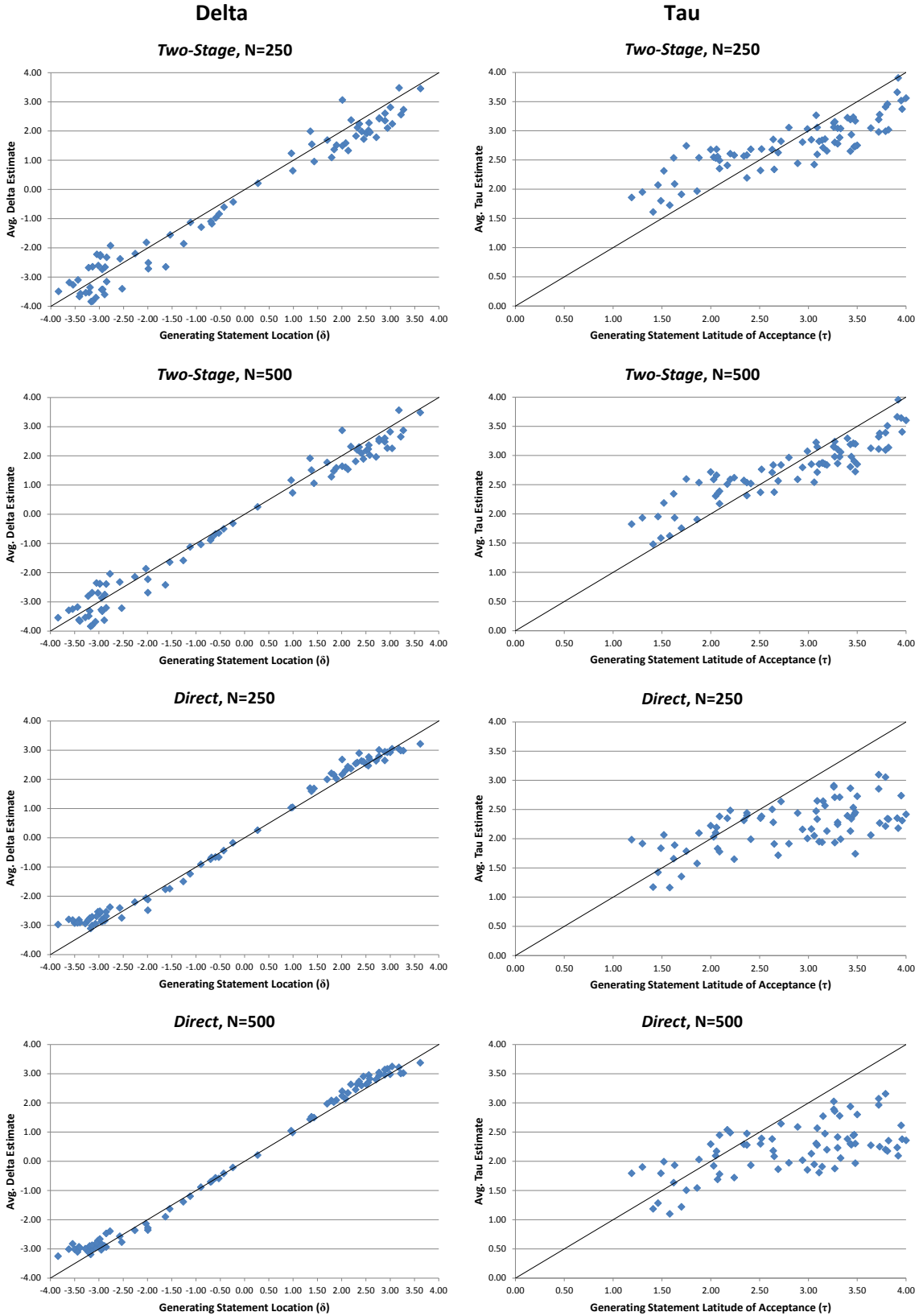


Figure 8.1. Average estimates of statement location and latitude of acceptance parameters as a function of the corresponding generating parameter value for 4-D HCM-RANK conditions.

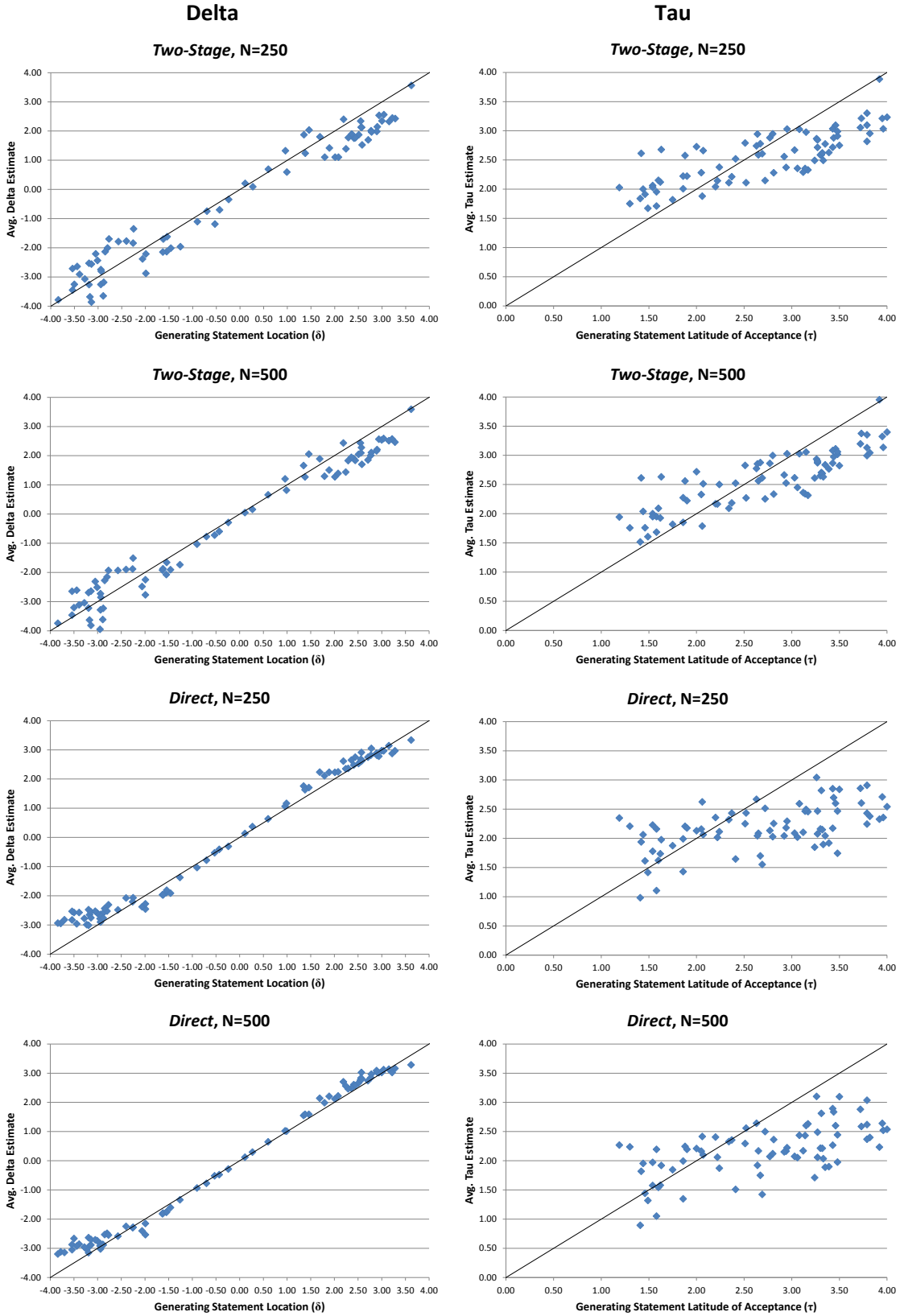


Figure 8.2. Average estimates of statement location and latitude of acceptance parameters as a function of the corresponding generating parameter value for 8-D HCM-RANK conditions.

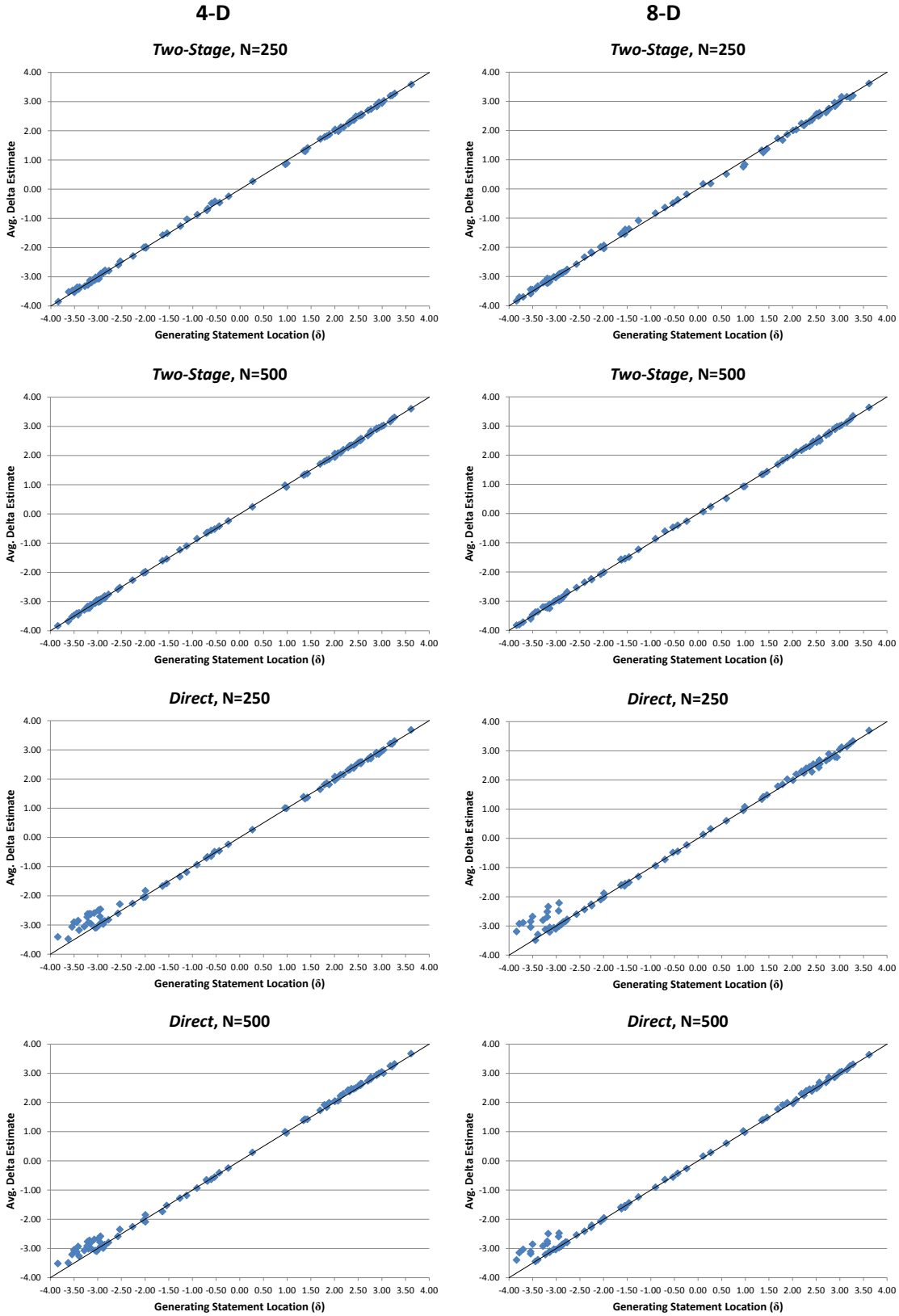


Figure 8.3. Average estimates of statement location parameters as a function of the corresponding generating parameter value for 4-D and 8-D SHCM-RANK conditions.

Testing Study Hypotheses

This study offered six hypotheses related to statement and person parameter recovery using the SHCM- and HCM-RANK models. Hypotheses 1 and 2 proposed that parameter recovery would be more accurate in the large sample-size conditions and for the 4-D tests, respectively. These hypotheses were tested using a MANOVA with sample size and number of dimensions as the between subject factors and the correlation and RMSEs for each of the three parameters as dependent variables. The results for the multivariate tests are provided in Table 8.4, where it can be seen that statistically significant effects were found for both factors. The number of dimensions (eta squared = .92) had a stronger effect than sample size (eta squared = .40).

Table 8.4
MANOVA Table for Multivariate Tests of Between Subjects Effects for Study 1 Hypotheses 1 and 2

Effect	Test	Value	F	Hypothesis df	Error df	Sig.	Partial Eta Squared
Sample Size	Pillai's Trace	0.40	26.19	6	232	0.00	0.40
	Wilks' Lambda	0.60	26.19	6	232	0.00	0.40
	Hotelling's Trace	0.68	26.19	6	232	0.00	0.40
	Roy's Largest Root	0.68	26.19	6	232	0.00	0.40
Number of Dimensions	Pillai's Trace	0.92	424.06	6	232	0.00	0.92
	Wilks' Lambda	0.08	424.06	6	232	0.00	0.92
	Hotelling's Trace	10.97	424.06	6	232	0.00	0.92
	Roy's Largest Root	10.97	424.06	6	232	0.00	0.92

Because both main effects were significant, univariate tests for individual statistics were examined and are presented in Table 8.5. The univariate tests for sample size were significant for δ recovery statistics and θ RMSEs (other statistics were nonsignificant after Bonferroni corrections for the number of comparisons) and the eta squared effect size estimates were small.

These results partially support Hypothesis 1, as parameter recovery was more accurate for the large sample size conditions for the δ parameter, but not for the τ or θ parameters. Examining the univariate tests for number of dimensions, significant effects were found for all recovery statistics except the τ parameter. The eta square effect sizes were large for the θ parameters, indicating that large improvements were made when fewer dimensions were assessed, presumably because more statements reflecting each dimension were administered. This indicates that trait recovery can be improved by increasing test length. Because τ parameters were not recovered more accurately in 4-D conditions than in 8-D, Hypothesis 2 was partially supported.

Table 8.5
Results for Univariate Tests of Between Subjects Effects for Study 1 Hypotheses 1 and 2

Source	Dependent Variable	SS	df	Mean Square	F	Sig.	Partial Eta Squared
Sample Size	δ RMSE	0.34	1	0.34	58.63	0.00	0.20
	τ RMSE	0.06	1	0.06	1.49	0.22	0.01
	δ Correlation	0.00	1	0.00	51.33	0.00	0.18
	τ Correlation	0.10	1	0.10	4.91	0.03	0.02
	θ RMSE	0.00	1	0.00	17.07	0.00	0.07
	θ Correlation	0.00	1	0.00	5.47	0.02	0.02
Number of Dimensions	δ RMSE	0.22	1	0.22	39.32	0.00	0.14
	τ RMSE	0.03	1	0.03	0.65	0.42	0.00
	δ Correlation	0.00	1	0.00	39.39	0.00	0.14
	τ Correlation	0.01	1	0.01	0.46	0.50	0.00
	θ RMSE	0.29	1	0.29	1845.85	0.00	0.89
	θ Correlation	0.11	1	0.11	2192.47	0.00	0.90

Note. RMSE = average root mean square error.

Hypotheses 3 and 4 proposed that when considering person parameter recovery no differences would be found between *direct* and *two-stage* estimation conditions, nor would

differences be found between HCM and SHCM conditions. Consistent with these hypotheses, the results of a MANOVA, shown in Table 8.6, indicate that no significant effects were found.

Table 8.6
MANOVA Table for Multivariate Tests of Between Subjects Effects for Study 1 Hypotheses 3 and 4

Effect	Test	Value	F	Hypothesis df	Error df	Sig.	Partial Eta Squared
Estimation Strategy	Pillai's Trace	0.01	2.38	2	476	0.09	0.01
	Wilks' Lambda	0.99	2.38	2	476	0.09	0.01
	Hotelling's Trace	0.01	2.38	2	476	0.09	0.01
	Roy's Largest Root	0.01	2.38	2	476	0.09	0.01
	Root						
Model	Pillai's Trace	0.01	1.59	2	476	0.21	0.01
	Wilks' Lambda	0.99	1.59	2	476	0.21	0.01
	Hotelling's Trace	0.01	1.59	2	476	0.21	0.01
	Roy's Largest Root	0.01	1.59	2	476	0.21	0.01
	Root						

Hypothesis 5 proposed that there would be significant differences in statement parameter recovery between *two-stage* and *direct* estimation conditions. This hypothesis was examined two ways. First, the recovery scatterplots in Figures 8.1, 8.2, and 8.3 were examined visually. There was little difference between estimation strategies for δ parameters, but τ parameters were recovered better in *two-stage* conditions. To test Hypothesis 5 statistically, a MANOVA was conducted with estimation strategy and statement parameter (δ or τ) as between subjects factors, and the RMSE and correlation as dependent variables. The results for the multivariate tests are provided in Table 8.7, where it can be seen that statistically significant effects were found for both factors as well as an interaction.

Table 8.7

MANOVA Table for Multivariate Tests of Between Subjects Effects for Study 1 Hypothesis 5

Effect	Test	Value	F	Hypothesis df	Error df	Sig.	Partial Eta Squared
Estimation Strategy	Pillai's Trace	0.83	1806.68	2	715	0.00	0.83
	Wilks' Lambda	0.17	1806.68	2	715	0.00	0.83
	Hotelling's Trace	5.05	1806.68	2	715	0.00	0.83
	Roy's Largest Root	5.05	1806.68	2	715	0.00	0.83
	Root						
Statement Parameter	Pillai's Trace	0.97	12482.20	2	715	0.00	0.97
	Wilks' Lambda	0.03	12482.20	2	715	0.00	0.97
	Hotelling's Trace	34.92	12482.20	2	715	0.00	0.97
	Roy's Largest Root	34.92	12482.20	2	715	0.00	0.97
	Root						
Estimation Strategy * Statement Parameter	Pillai's Trace	0.84	1885.31	2	715	0.00	0.84
	Wilks' Lambda	0.16	1885.31	2	715	0.00	0.84
	Hotelling's Trace	5.27	1885.31	2	715	0.00	0.84
	Roy's Largest Root	5.27	1885.31	2	715	0.00	0.84
	Root						

Because tests for both main effects and interactions were significant, univariate tests for individual statistics were examined and are presented in Table 8.8. The univariate tests were all significant and the effect sizes were large. Given the significant interaction between estimation strategy and statement parameter for both RMSE and correlation, the interactions were plotted in Figure 8.4. For δ , there is no discernible difference between *two-stage* and *direct* estimation conditions. However, for τ , the RMSE is clearly smaller and the correlation larger in the *two-stage* conditions. This effect indicates that if accurate recovery of both statement location and latitude of acceptance parameters is important, then a *two-stage* estimation approach is preferable. Finally, note that because Hypothesis 6 proposed that δ parameters would be estimated more accurately than τ parameters, these findings provide support for both Hypothesis 5 and Hypothesis 6.

Table 8.8

Results for Univariate Tests of Between Subjects Effects for Study 1 Hypothesis 5

Source	Dependent Variable	SS	df	Mean Square	F	Sig.	Partial Eta Squared
Estimation	RMSE	5.74	1	5.74	319.48	0.00	0.31
Strategy	Correlation	2.74	1	2.74	3554.68	0.00	0.83
Statement	RMSE	16.79	1	16.79	934.50	0.00	0.57
Parameter	Correlation	18.18	1	18.18	23584.16	0.00	0.97
Estimation	RMSE	6.14	1	6.14	341.60	0.00	0.32
Strategy *	Correlation	2.86	1	2.86	3713.13	0.00	0.84
Statement							
Parameter							

Note. RMSE = average root mean square error.

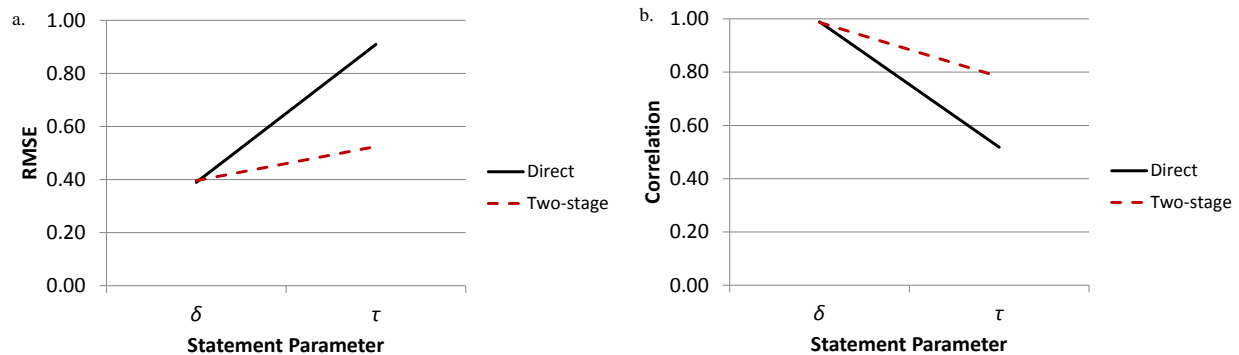


Figure 8.4. The interaction between statement parameters and estimation strategy for Study 1 conditions.

Study 1 Result Summary and Preview

This study examined the accuracy of HCM-RANK and SHCM-RANK statement and person parameter recovery by constructing MFC item tetrads and using a *direct* estimation or *two-stage* estimation process. Overall, statement location parameters were well estimated using both approaches, while statement latitude of acceptance parameters showed markedly lower recovery accuracy across the studied conditions. Statement parameters were more accurately estimated with larger sample sizes, but statement locations were still reasonably well recovered in the N-500 conditions (particularly the SHCM). Although the correlation between generating

and estimated person parameters never reached .90, correlations in the mid to high .80s indicate fairly good recovery considering test length. By increasing test length it is expected that both statement and person parameter recovery accuracy would also increase.

These results demonstrate the efficacy of the HCM-RANK and SHCM-RANK MCMC estimation methods for MFC item tetrads and are consistent with previous studies focusing specifically on trait score recovery. Stark, Chernyshenko, and Drasgow (2005) reported correlations between generating and estimated trait scores ranging from .77 to .86 for a 2-D pairwise preference test with 20 statements representing each dimension. Additionally, Stark, Chernyshenko, Drasgow, and White (2012) found correlations of .68 to .92 for simulations of 2-D to 25-D pairwise preference tests with uncorrelated latent dimensions. Using the Thurstonian approach, Brown and Maydeu-Olivares (2011) found correlations ranging from .80 to .95 across simulations of 5-D tests using item pairs, triplets, and tetrads. Most comparable to the current study, de la Torre et al. (2012) found average correlations of .86 and .87 for 4-D pairwise preference and tetrad-ranking conditions, respectively, when utilizing the GGUM as the foundation for data generation and scoring. Results from the current study show comparable correlations between generating and estimated latent trait scores, ranging from .83 to .88 across the *two-stage* and *direct* estimation approaches.

One finding of particular interest in this study is that there were no significant differences between estimation strategies in regard to person parameter recovery, indicating that MFC scales can be constructed and administered without the need to for statement precalibration. A sufficient number of MFC responses, however, must first be gathered before statement parameter estimation and person scoring can occur. In Chapter 9, one potential strategy for obtaining initial

score estimates prior to the estimation of statement parameters is described, and a simulation study is performed to examine the efficacy of the approach.

CHAPTER 9:
STUDY 2: EXAMINING SHCM-RANK TRAIT SCORE RECOVERY
USING SME LOCATION ESTIMATES

Item response theory methods offer many benefits for test development, but a key drawback is that large samples are needed to accurately estimate the item parameters that are used for scoring. With 250 examinees considered a fairly small sample in the IRT realm, the cost of developing one item can easily exceed \$100, thus forcing organizations to accept longer lags for return on investment or, in the case of admissions and licensure testing, forcing examinees to pay higher prices.

In Study 1, two approaches to item parameter estimation were examined in connection with the scoring of MFC rank responses. In *direct* estimation conditions, an MFC tetrad test was administered to a large sample of respondents and item and person parameters were estimated simultaneously (directly) from the rank responses. In *two-stage* conditions, individual statements were administered to a large sample of respondents and calibrated using a unidimensional single-statement model; then the statement parameters from the precalibration were used to score MFC rank responses. Consequently, despite procedural differences, both direct and two-stage estimation used samples of 250 or more for estimating the item parameters that were needed for scoring.

In recognition of this practical limitation and the desire for organizations to expedite test development and launch, Stark, Chernyshenko, and Guenole (2011) explored the use of subject matter expert (SME) location estimates in place of marginal maximum likelihood (MML)

location parameter estimates with the Zinnes and Griggs (ZG; 1974) unidimensional pairwise preference model. They found that trait scores based on SME locations correlated .97 and .93 with trait scores based on MML locations, even though the correlations between the SME and MML locations were just .83 and .62, respectively. Moreover, in a follow-up computer simulation, the researchers found that trait score estimates based on SME locations, which correlated only .6 with the true locations parameters, were comparable to trait scores calculated using MML location estimates based on samples of 500 examinees. Together, these results suggest that SME location estimates might serve as viable proxies for IRT location estimates in the early stages of testing and possibly beyond. An important follow-up question is whether these results will generalize to other models and more complex assessments.

Models that have been explored for MFC testing, to date, have all involved multiple parameters. Stark (2002) and de la Torre et al. (2012) computed *most like* probabilities based on the Generalized Graded Unfolding Model (GGUM; Roberts, Donoghue, & Laughlin, 2000), which has three parameters for every statement (location, threshold, and discrimination). Similarly, Brown and Maydeu-Olivares (2011) used a normal ogive model involving two parameters per statement (an intercept and a factor loading). Consequently, research is needed to explore whether simpler models, involving just location parameters, can provide effective scoring of MFC responses, and to what extent estimation accuracy will diminish if SME location estimates are substituted for IRT location parameters.

The SHCM-RANK model is a natural choice for this type of study. Like the ZG model, explored by Stark et al. (2011) the SHCM has just one parameter per statement, representing its location on the trait continuum. Thus, Study 2 of this dissertation explores whether MFC test

construction and scoring can be streamlined by substituting SME location estimates for MCMC-based SHCM statement locations, as described below.

Simulation Study

Study Design

A Monte Carlo study was conducted to explore the efficacy of SHCM-RANK trait score recovery with 4-D and 8-D MFC tests using SME-based SHCM location parameter estimates having varying correlations with the true location parameters. The simulation involved two independent variables with levels, as shown:

- 1) Dimensionality of MFC assessment:
 - a) 4 dimensions; and
 - b) 8 dimensions.
- 2) Location parameters used for SHCM-RANK scoring:
 - a) TRUE location parameters;
 - b) SME90: location estimates correlating .90 with true location parameters;
 - c) SME80: location estimates correlating .80 with true location parameters;
 - d) SME70: location estimates correlating .70 with true location parameters;
 - e) SME60: location estimates correlating .60 with true location parameters; and
 - f) SME50: location estimates correlating .50 with true location parameters.

Simulation Procedure

- 1) For each dimension in the MFC test, SME location parameter estimates having the desired correlation with the true location parameters were created as follows: An appropriately sized vector of values (\mathbf{z}) was sampled from an independent standard normal distribution and the following transformation was applied, $\mathbf{s} = \rho\mathbf{t} + \sqrt{(1 - \rho^2)}\mathbf{z}$,

where \mathbf{t} represents the true location parameters, ρ represents the desired correlation, and \mathbf{s} represents the resulting vector of SME location estimates.

- 2) For the designated number of dimensions in the MFC test, trait scores for 1,000 examinees were sampled from independent standard normal distributions. SHCM-RANK responses were generated using the true trait scores and true location parameters, as described in Study 1.
- 3) The SHCM-RANK responses were scored using the TRUE or SME location estimates and the results were saved.
- 4) Steps 1 through 3 were repeated until 30 replications were performed. Indices of estimation accuracy were then computed.

Indices of Estimation Accuracy

As in Study 1, trait score recovery were examined using a combination of Pearson correlations between average estimated and true trait scores and root mean square errors given by Equation 7.3.

Hypotheses

Based on Stark et al. (2011), who used SME location estimates to score unidimensional forced choice scales, the follow hypotheses are proposed:

1. Trait scores will be estimated more accurately with 4-D tests than with 8-D tests (as indicated by significantly larger Pearson correlations between estimated and true trait scores and significantly lower RMSE statistics), because keeping test length constant (20 items) means that each dimension in the 8-D test is represented by fewer statements.
2. Trait score estimation accuracy will decrease as the correlation between the SME locations and TRUE locations decreases.

These hypotheses were tested using MANOVA and, for Hypothesis 2, orthogonal polynomial contrasts to test the linear trend.

CHAPTER 10:

STUDY 2 RESULTS

The purpose of this study was to examine whether SME location estimates containing varying degrees of error can be used effectively to score MFC responses with the SHCM-RANK model. Correlations between estimated and generating trait scores were computed as were root mean square errors (RMSE). Table 10.1 presents the parameter recovery results for the 12 simulation conditions, averaged across replications and dimensions. As expected, recovery was best with the TRUE parameters and better with 4-D than 8-D tests in the corresponding SME conditions. Importantly, parameter recovery diminished only minimally each time the correlation between the true and SME location estimates was decreased by .1, indicating the robustness of trait scores to measurement error. Remarkably correlations between the true and estimated trait scores were at or above .8 even when SME locations correlated only .7 with the true values.

Testing Study Hypotheses

Two hypotheses were proposed for this study. Hypothesis 1 stated that person parameter recovery would be more accurate with 4-D measures than 8-D measures. This hypothesis was tested using a MANOVA with number of dimensions as the between subjects factor and the correlation and RMSE statistics for person parameters as dependent variables. The multivariate test results in Table 10.2 show that the effect for dimensions was significant, with a moderate effect size ($\eta^2 = .33$). Consequently, univariate tests were conducted, and these results are presented in Table 10.3. As can be seen in the table, significant effects were found for both the correlation and RMSE, providing support for Hypothesis 1.

Table 10.1

Study 2 Trait Recovery Results using Simulated SME Locations

Number of Dimensions	Location Parameters Used for Scoring	Recovery Statistic	
		Correlation	RMSE
4	TRUE	0.88	0.47
	SME90	0.87	0.50
	SME80	0.86	0.53
	SME70	0.84	0.58
	SME60	0.82	0.61
	SME50	0.79	0.65
8	TRUE	0.84	0.54
	SME90	0.83	0.56
	SME80	0.82	0.59
	SME70	0.80	0.62
	SME60	0.79	0.65
	SME50	0.76	0.68

Note. TRUE = Known generating statement parameters used for scoring. SME90, SME80, SME70, SME60, SME50 = SME location estimates simulated to correlate .90, .80, .70, .60, and .50, respectively, with the known statement parameters.

Table 10.2

MANOVA Table for Multivariate Tests of Between Subjects Effects for Study 2 Hypothesis 1

Effect	Test	Value	F	Hypothesis df	Error df	Sig.	Partial Eta Squared
Number of Dimensions	Pillai's Trace	0.33	88.501b	2	357	0.00	0.33
	Wilks' Lambda	0.67	88.501b	2	357	0.00	0.33
	Hotelling's Trace	0.50	88.501b	2	357	0.00	0.33
	Roy's Largest Root	0.50	88.501b	2	357	0.00	0.33
	Root						

Table 10.3

Results for Univariate Tests of Between Subjects Effects for Study 2 Hypothesis 1

Source	Dependent Variable	SS	df	Mean Square	F	Sig.	Partial Eta Squared
Number of Dimensions	θ RMSE	0.25	1	0.25	71.24	0.00	0.17
	θ Correlation	0.12	1	0.12	121.51	0.00	0.25

Note. RMSE = average root mean square error.

Hypothesis 2 proposed that trait estimation accuracy would decrease as the correlation between SME and TRUE locations decreased. Consistent with a visual inspection of the results,

orthogonal polynomial contrasts for a linear trend indicated statistically significant effects for RMSE, $F(1, 354) = 939.94, p < .01$, and correlation, $F(1, 354) = 688.66, p < .01$. As shown in Figure 10.1, the correlation decreased steadily and RMSE increased steadily as error was introduced into the location estimates.

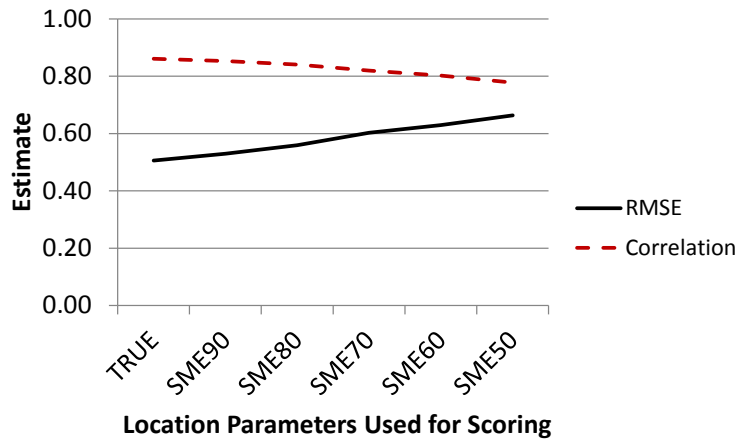


Figure 10.1. Linear trend results for root mean square error (RMSE) and correlation statistics across Study 2 conditions.

Study 2 Result Summary and Preview

One limitation to the use of MFC measures in research and practice is the relatively large samples needed to estimate statement parameters for scoring. To address this limitation, this study examined whether SME estimates of statement location could be used in lieu of IRT parameters to streamline test development based on the SHCM-RANK model. The results of this simulation suggest that even moderately accurate statement location estimates, correlating .60 to .70 with the true parameters, can yield trait scores that correlate .80 with their true values. Also, accuracy should improve as test length increases, given the better recovery in the 4-D conditions than in the 8-D. Although these simulation results support the viability of using SME location estimates for scoring, research is needed to examine efficacy with human research participants.

Study 3 was designed to initiate work in that domain, as a prelude to a more comprehensive future investigation.

CHAPTER 11

STUDY 3:

A CONSTRUCT VALIDITY INVESTIGATION OF SHCM-RANK SCORES

The simulation studies in previous chapters examined the efficacy of the MCMC algorithms for recovering HCM-RANK and SHCM-RANK item and person parameters. Such simulation work is essential for refining algorithms, developing evidence-based guidelines for test construction, and making projections about reliability of MFC tests in field applications. However, empirical research is ultimately needed to provide an external check on the validity of those inferences.

This chapter describes a small construct validity study to complement the simulation findings. It was intended only to provide a stepping stone for future validity investigations. In a nutshell, I examined the convergent and discriminant validities of four single-statement personality measures and a 4-D MFC tetrad measure that was scored three ways, and the relationships of the scores with external criteria. The correlations between the Likert-type sum scores for the respective single-statement measures and the MCMC-based scores for the tetrad measure serve as indicators of convergent validity, and the cross-dimension correlations serve as indicators of discriminant validity. Finally, the correlation between the dimension scores for each approach and related outcome variables provide additional indications of the efficacy of the MFC tetrad methods.

Participants and Measures

The empirical sample consisted of 253 individuals who anonymously completed an online personality questionnaire as part of a larger data collection project (Loo, manuscript in progress) and three SMEs who were asked to estimate the locations of the personality statements included in that questionnaire. It was expected that three SMEs would be sufficient for this purpose, given that Stark et al. (2011) used just two and found that trait scores based on the SME judgments correlated above .9 with trait scores based on marginal maximum likelihood estimates; and their Study 2 found only a marginal decrease in person parameter recovery as SME rating error increased.

The online participants responded to a personality questionnaire involving single-statement items and tetrads measuring four broad personality factors: extraversion, openness to experience, conscientiousness, and emotional stability. The 12-item single-statement measures of each factor were created by selecting statements from the International Personality Item Pool (IPIP; Goldberg et al., 2006). This single-statement measure is presented in Appendix C. Participants indicated their level of agreement with each statement on a 1 (strongly disagree) to 4 (strongly agree) scale. The 4-D MFC measure was created by rearranging the 48 personality statements used in Study 1 into 12 tetrads, which respondents ranked from 1 (most like me) to 4 (least like me). An effort was made to balance the social desirability of the statements within each tetrad and, in the aggregate, to include statements that spanned the trait continua from low to high. This tetrad measure is presented in Appendix D.

The SME estimates of statement locations were obtained in the manner described by Stark et al. (2011). The SMEs for this study were three individuals with postgraduate degrees in Industrial-Organizational Psychology and experience with item writing and the personality

constructs of interest. The 48 personality statements measuring 4 dimensions were shuffled and presented to three SMEs with instructions to consider each statement independently and indicate its standing on the trait continuum using a 1 (very low) to 7 (very high) scale. The ratings were then averaged across SMEs and transformed to a -3.0 to 3.0 scale for SHCM-RANK scoring.

To examine the relationship of the personality scores to external criteria, information on participants' organizational citizenship (OCB) and counterproductive work behaviors (CWB) were gathered using both self-report responses and coworker ratings. Because self-report OCB and CWB scores may be contaminated by biases similar to those that distort personality scores, coworker ratings for 170 of the participants were examined as a secondary source of participants' behaviors. OCB was assessed using a 10-item measure of personal OCB ("Went out of the way to give coworker encouragement or express appreciation"; $\alpha = .78$) from a checklist developed by Fox, Spector, Goh, Bruurseman, and Kessler (2012). Participants and coworkers responded to this measure using a five-point Likert-type format on a 1 (never) to 5 (every day) scale. Participant CWB ("Stolen something belonging to your employer"; $\alpha = .95$) was measured using Spector et al.'s (2006) 32-item Counterproductive Work Behavior Checklist. Participants responded to this measure by indicating how often they have done a series of behaviors on their job. Responses were gathered using a five-point Likert-type format on a 1 (never) to 5 (every day) scale.

Although a recent meta-analysis found a significant relationship for emotional stability ($r = -.20$) and conscientiousness ($r = -.19$) with self-report CWB (Berry, Ones, & Sackett, 2007), the use of observer-report CWB indicates very little relationship with emotional stability ($r = -.04$) (Berry, Carpenter, & Barratt, 2012). Similarly, meta-analytic results indicate that self-report emotional stability ($r = .10$), conscientiousness ($r = .14$), and openness ($r = .11$) scores

moderately relate to OCB (Chiaburu, Oh, Berry, Li, & Gardner, 2011), but studies involving observer-report OCB indicate a significant relationship only for conscientiousness ($r = .13$) (Bourdage, Lee, Lee, & Shin, 2012; Connelly & Hülshager, 2012). Collectively, these findings suggest that using self-report Likert-type measures of predictor and criterion variables may inflate the relationships of interest, so research is needed to see whether MFC measures will be more resistant to potential response sets.

Analyses

Personality scores for the 253 online participants were calculated four ways. The four single-statement measures were scored by reverse coding negatively worded statements and summing the selected category codes to obtain LIKERT trait scores for each participant. Then the MFC tetrad rank responses were scored three ways:

- 1) HCM-RANK trait scores were obtained by directly (simultaneously) estimating item and person parameters from the rank responses;
- 2) SHCM-RANK trait scores were obtained by directly (simultaneously) estimating item and person parameters from the rank responses; and
- 3) SHCM-RANK-SME trait scores were obtained by scoring the rank responses using SME location estimates.

Finally, scale scores for the OCB and CWB measures were calculated through the traditional approach of reverse coding negatively worded statements and summing across the items composing each measure.

The correlations between these sets of scores were used to examine convergent and discriminant validity. High correlation between the respective LIKERT and HCM-RANK trait scores provides support for the new IRT model and its MCMC implementation. High correlation

between those scores and the SHCM-RANK scores signifies that the simpler one-parameter model should be carefully considered for future field applications. High correlations between the previous sets of scores and the SHCM-RANK-SME scores provides evidence that SME location estimates can be also used to streamline *multidimensional* forced choice test development, supporting Stark et al.'s (2011) findings for unidimensional forced choice tests. Lower intercorrelations among the dimensions assessed with tetrads signals better discriminant validities, perhaps due to reduced social desirability response bias. Finally, similar correlations between LIKERT, HCM-RANK, SHCM-RANK, and SHCM-RANK-SME scores and related outcome measures indicates that trait recovery is comparable across MFC strategies when compared to a traditional Likert approach, providing evidence of the validity of those scores.

Hypotheses

Chernyshenko et al. (2009) demonstrated that IRT-based multidimensional pairwise preference, unidimensional pairwise preference, and single-statement personality tests administered under “honest” conditions have similar convergent, discriminant, and predictive validities. In addition, Stark et al. (2011) showed that trait scores for unidimensional pairwise preference tests are fairly robust to error in statement parameter estimates stemming from calibrating small samples or substituting SME estimates of statement locations. With these findings in mind, the following hypotheses were proposed:

1. Comparing HCM-RANK, SHCM-RANK, and SHCM-RANK-SME trait scores: The monotrait heteromethod correlations will be high, and similar heterotrait monomethod correlations will be observed across the approaches.
2. The monotrait heteromethod correlations between the LIKERT trait scores and HCM-RANK, SHCM-RANK, and SHCM-RANK-SME trait scores will be high.

3. The heterotrait monomethod correlations for LIKERT trait scores will be higher than those for the HCM-RANK, SHCM-RANK, and SHCM-RANK-SME approaches.
4. Examining the criterion measures, personality scores for both LIKERT and MFC tetrad scoring will show moderate correlations with self-report OCB and CWB scores, and small correlations with coworker-report OCB and CWB scores.

As the HCM-RANK, SHCM-RANK, and SHCM-RANK-SME approaches score the same response data using different methods, the hypotheses offered here were examined through the creation and inspection of a multi-trait multi-method matrix of correlations. Additionally, the correlations between the personality scores and the criterion scores were compared across formats to examine their comparability.

CHAPTER 12:

STUDY 3 RESULTS

This study was conducted as initial foray into HCM-RANK and SHCM-RANK MFC test construction and scoring with human research participants. Table 12.1 presents the multi-trait multi-method matrix for emotional stability, conscientiousness, openness, and extraversion obtained using single-statement measures and MFC item tetrads that were scored using three approaches. The bold values along the diagonals of each scoring format highlight the monotrait heteromethod correlations. As can be seen in the table, these correlations were generally large, with values ranging from .60 to .94. The correlations among trait scores were lowest for the SHCM-RANK and SHCM-RANK-SME methods. Overall, the high monotrait heteromethod correlations support the first part of Hypothesis 1.

In Table 12.1, it can be seen that the correlations between LIKERT and MFC scores were highest for emotional stability and extraversion and lowest for conscientiousness and openness. However, the correlations were low overall, ranging from just .26 to .61, which does not support Hypothesis 2 concerning convergent validity.

Given this finding, it is important to consider potential explanations. One explanation is that the statements measuring each construct were too different across measures, so different facets or aspects of personality may have been emphasized. For example, Heggstad et al. (2006) found correlations ranging from .75 to .87 between MFC tetrads and single-statement measures when items had overlapping content, but the correlations decreased to a range of .58 to .71 when

overlap was eliminated. Similarly, Chernyshenko et al. (2009) found correlations across formats ranging from .54 to .75 with a modest degree of overlap.

A second possible explanation for the low convergent validity is the LIKERT measures were more influenced by response distortion than the MFC measure, and the MFC measure yielded more accurate trait scores. Of course, an alternative explanation is that the MFC scores were inaccurately estimated because the measure was too short to provide sufficient test information, or the examinees found it more difficult and responded haphazardly. It is also possible that all of these explanations are relevant to some extent.

Turning to the heterotrait monomethod correlations in Table 12.1, it can be seen that there is some inconsistency in the relationship among the personality dimensions across the HCM-RANK, SHCM-RANK, and SHCM-RANK-SME strategies. Both the HCM-RANK and the SHCM-RANK-SME scores showed significant correlations between emotional stability and openness, while SHCM-RANK estimates did not. Similarly, both SHCM-RANK and SHCM-RANK-SME scores showed significant correlations between openness and extraversion, but in the opposite direction. Consequently, the consistency of heterotrait monomethod correlations proposed in Hypothesis 1 was not supported. The heterotrait monomethod correlations were, however, larger for LIKERT scores when compared to the MFC tetrad scores, indicating some ability for the forced choice models to reduce score inflation commonly found in self-report measures. This pattern of results supports Hypothesis 3.

Table 12.1

Study 3 Correlations Between Personality Facet Scores Obtained using Single-Statement Responses and MFC Responses Scored Three Ways

Format	Construct	LIKERT				HCM-RANK				SHCM-RANK				SHCM-RANK-SME			
		E.S.	Con.	Op.	Ex.	E.S.	Con.	Op.	Ex.	E.S.	Con.	Op.	Ex.	E.S.	Con.	Op.	Ex.
LIKERT	Emotional Stability	.41**															
	Conscientiousness		.31**														
	Openness	.15*		.11													
HCM-RANK	Emotional Stability	.52**	.11	.00	.09												
	Conscientiousness	-.01	.25**	-.08	-.14*	-.02											
	Openness	.15*	.08	.36**	-.01	.18**	-.15*										
SHCM-RANK	Emotional Stability	.53**	.11	.01	.09	.94**	.00	.17**	.04								
	Conscientiousness	-.07	.26**	-.05	-.17**	-.11	.94**	-.13*	-.18**	-.06							
	Openness	.01	.01	.28**	-.15*	.04	-.03	.75**	-.22**	.07	.03						
SHCM-RANK-SME	Emotional Stability	.55**	.11	.06	.16**	.94**	-.08	.23**	.10	.91**	-.16**	.07	-.02				
	Conscientiousness	.04	.27**	.00	-.06	-.01	.88**	-.02	-.07	.00	.86**	.03	-.01	.01			
	Openness	.15*	.01	.34**	.09	.14*	-.25**	.72**	.01	.13*	-.21**	.60**	.04	.26**	.01		
	Extraversion	-.05	-.13*	.06	.55**	-.09	-.23**	.00	.73**	-.08	-.24**	-.09	.75**	.05	-.05	.22**	

Note. * = $p < .05$; ** = $p < .01$; Bold coefficients indicate monotrait heteromethod correlations; LIKERT = Single-statement gathered via a Likert-type scale; HCM-RANK = Hyperbolic Cosine Model for Rank order responses; SHCM-RANK = Simple Hyperbolic Cosine Model for Rank order data; SHCM-RANK-SME = Simple Hyperbolic Cosine Model for Rank order responses using subject matter expert ratings for scoring; E.S. = Emotional Stability; Con. = Conscientiousness; Op. = Openness; Ex. = Extraversion;

Table 12.2 presents the criterion-related validity results for the LIKERT, HCM-RANK, SHCM-RANK and SHCM-RANK-SME scores. Examining the correlations between personality dimensions and self-report OCB and CWB, it can be seen that there was a strong relationship between the criteria and LIKERT scores. Single-statement LIKERT scores showed significant correlations between self-report OCB and all dimensions except emotional stability. Similarly, LIKERT scores showed significant correlations with self-report CWB for all personality dimensions except extraversion. Finding no relationship between LIKERT extraversion scores and self-report OCB was a surprise, as meta-analyses have indicated a moderate relationship between the constructs. This also raises construct validity questions about the LIKERT emotional stability scores. Considering the significant correlations between LIKERT personality scores and self-report external criteria, the magnitudes of the relationships are larger than what is typically found in other research and may indicate inflation due to a general self-report response bias. In particular, LIKERT scores for conscientiousness showed an unexpectedly strong correlation with self-report CWB ($r = -.37$), although the relationship was also fairly strong for the MFC methods. Finally, examining the HCM-RANK, SHCM-RANK, and SHCM-RANK-SME relationships with self-report OCB and CWB, it is apparent that the only relationship worth noting is conscientiousness with CWB. That the other expected relationships were near zero suggests that difficulties were encountered in the MFC component of this study, which highlights the need for a more comprehensive future investigation.

Table 12.2

Study 3 Criterion-Related Validities of Personality Facets Obtained using Single-Statement Responses and MFC Responses Scored Three Ways

Format	Construct	Criterion			
		Self-Report		Coworker-Report	
		OCB	CWB	OCB	CWB
LIKERT	Emotional Stability	.00	-.21**	-.04	-.15*
	Conscientiousness	.18**	-.37**	.04	-.24**
	Openness	.13*	-.20**	-.10	-.02
	Extraversion	.14*	-.04	.08	-.05
HCM-RANK	Emotional Stability	.06	-.03	-.04	.02
	Conscientiousness	-.02	-.13*	.10	.03
	Openness	.09	-.07	-.06	-.07
	Extraversion	-.01	.06	.03	.06
SHCM-RANK	Emotional Stability	.04	-.03	-.03	.00
	Conscientiousness	-.03	-.15*	.11	-.01
	Openness	.00	.03	-.08	-.08
	Extraversion	-.05	.01	.01	.00
SHCM-RANK-SME	Emotional Stability	.06	-.02	-.10	.01
	Conscientiousness	-.02	-.15*	.00	.00
	Openness	.05	-.03	-.17*	-.02
	Extraversion	.02	.10	-.06	.02

Note. * = $p < .05$; ** = $p < .01$; LIKERT = Single-statement gathered via a Likert-type scale; HCM-RANK = Hyperbolic Cosine Model for Rank order responses; SHCM-RANK = Simple Hyperbolic Cosine Model for Rank order data; SHCM-RANK-SME = Simple Hyperbolic Cosine Model for Rank order responses using subject matter expert ratings for scoring; OCB = Organizational citizenship behaviors; CWB = Counterproductive work behaviors.

Because self-report measures may show inflated correlations with self-report criteria, examining the relationship between self-report personality scores and coworker-report OCB and CWB provides an additional check on validities. The validity coefficients in the right two columns of Table 12.2 show that only LIKERT emotional stability and conscientiousness scores had significant relationships with coworker-report CWB, and only SHCM-RANK-SME openness scores had a significant relationship with coworker-report OCB. Overall, the LIKERT and MFC measures all had relatively weak criterion-related validities.

Study 3 Results Summary

Chapters 11 and 12 describe a small validity study that took an initial look at HCM-RANK MFC testing with human research participants. This study utilized an existing dataset to examine the convergent and discriminant validities of MFC tetrad scores, relative to traditional Likert-type scores, as well as relationships with external criteria. Overall, the results did not provide clear support for the construct validity of the HCM-RANK, SHCM-RANK, or SHCM-RANK-SME scores, but several possible explanations were offered for the unexpected findings. To prevent similar problems in future studies, researchers are encouraged to carefully pretest item tetrads, explore methods to compute MFC test information, and carefully pretest MFC measures using simulations to insure that test length is adequate for trait estimation.

Chapter 13:

DISCUSSION AND CONCLUSIONS

Although there has been an increased interest in the assessment of noncognitive constructs in educational and organizational settings, concerns surrounding the influence of response bias and response styles on these measures have limited their application in a wide range of settings. To address these concerns, researchers have examined alternative item presentation formats that may provide resistance to such biases. One such format is a multidimensional forced-choice item, which requires respondents to rank statements representing different dimensions in terms of preference, or alternatively to provide *most like* and/or *least like* responses. Several recent studies suggests that multidimensional forced choice measures reduce response biases and sets while providing normative information that can be used for decision making (Brown & Maydeu-Olivares, 2012; Heggstad, Morrison, Reeve, & McCloy., 2006; Stark, Chernyshenko, Drasgow, & White, 2012).

The purpose of this dissertation was to develop a new IRT model that can be applied to a variety of MFC item types. After deriving equations for the HCM-PICK and SHCM-PICK models for *most like* choices among a number of options, the HCM-RANK and SHCM-RANK models were developed based on the PICK probabilities. MCMC estimation algorithms were then developed for statement and person parameters, and a Monte Carlo simulation was performed to examine the efficacy of parameter recovery with *direct* and *two-stage* estimation approaches. The results indicated reasonable recovery of person parameters and excellent recovery of statement location parameters.

Follow-up studies were conducted to examine the potential for using SME estimates of statement locations for scoring, as well as the validity of MFC HCM-RANK methods with human research participants. The SME study indicated that location estimates can be used as proxies for IRT estimates in the early stages of MFC test development. However, more research is needed to look into difficulties that were encountered in the validity investigation.

Despite this, one motivation for the use of MFC items is to reduce the response biases and response styles evidenced in applied and cross-cultural studies. The construction of MFC item tetrads utilized for this dissertation balanced the social desirability of the constituent statements, reflecting a process intended to reduce item transparency and, presumably, response bias. Consequently, it is expected that the models presented here will provide the basis for empirically demonstrating this reduction in response bias in future studies.

Future Research

The *direct* estimation of statement parameters from MFC responses provides an opportunity to better understand how statements are evaluated within a context. This understanding will assist in the creation of parallel test forms, which are necessary for high-stakes uses. Additionally, *direct* estimation facilitates comparisons of item properties across subgroups, which is important in cross-cultural research and incumbent in some high stakes settings. Indeed, the SIOP Principles and Testing Standards (American Educational Research Association, American Psychological Association, & National Council on Measurement in Education, 1999) indicate that differential item functioning (DIF) analyses should be conducted when possible to promote bias-free measurement. Current strategies for detecting DIF with MFC items focus primarily on individual statements during item precalibration, but *direct* estimation

paves the way for comparisons of statement properties, for example, in the context of pairs and tetrads that have already been administered for assessment purposes.

Future research is also needed to develop a strategy for examining item and test information provided by the models described here. The derivation of information functions for the HCM-RANK and SHCM-RANK models may be particularly difficult as the complete response probability is based on a sequence of decisions where, in the case of a tetrad, there are 24 possible rankings. Instead, considering the information provided by an MFC item at the first *most like* selection using the HCM-PICK and SHCM-PICK may provide a more tractable avenue for developing item and test information functions. Estimation of the information provided by test items across each of the dimensions being assessed would be advantageous for test construction and evaluating the relative performance of different measures. Comparing the information provided by the Likert-type scales and the MFC measure in Study 3 would help determine whether the weak correlation resulted primarily from MFC measurement error.

Although Study 3 used a personality measure to illustrate the new MFC techniques, the methods developed in this dissertation offer interesting possibilities for situational judgment test (SJT) development and scoring. SJT items consist of scenarios followed by blocks of statements that represent different dimensions. Examinees are typically asked to indicate what they should/would do by choosing the best/most likely option or by ranking options from best/most likely to worst/least likely. Scores are typically obtained through a classical test theory approach involving SME estimates of statement effectiveness (i.e. location). Consequently, the HCM-PICK and HCM-RANK, as well as the corresponding SHCM, models may be useful for examining item quality, scoring, and constructing parallel forms.

Finally, although MFC methods have been discussed throughout this manuscript as a way of improving the quality of self-report data in noncognitive assessment, they can certainly be used for collecting observer reports for an equally large array of constructs. Borman et al. (2001) found that unidimensional forced choice measures reduced a variety of rater errors in the context of performance appraisal, so there is reason to believe that the MFC methods would also be effective, and researchers are encouraged to avidly explore these possibilities. The models presented here provide a basis for exploring these prospects in future research.

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APPENDIX A:

DERIVATION OF THE HCM-PICK

The PICK model developed by de la Torre et al. (2012) can be used to compute the probability of *most like* responses from a set of M alternatives. For a tetrad involving four statements, labeled A, B, C, and D, the probability of choosing the first statement in the i^{th} tetrad as *most like* is given by:

$$P_{(A>B,C,D)_i}(\theta_{d_A}, \theta_{d_B}, \theta_{d_C}, \theta_{d_D}) = \frac{P\{1,0,0,0\}}{P\{1,0,0,0\}+P\{0,1,0,0\}+P\{0,0,1,0\}+P\{0,0,0,1\}} = \frac{P_A(1)P_B(0)P_C(0)P_D(0)}{P_A(1)P_B(0)P_C(0)P_D(0)+P_A(0)P_B(1)P_C(0)P_D(0)+P_A(0)P_B(0)P_C(1)P_D(0)+P_A(0)P_B(0)P_C(0)P_D(1)}, \quad (\text{A1})$$

where:

i = the index for item tetrads, $i = 1$ to I ;

A, B, C, D = the labels for the statements in the item tetrad;

d = the dimension associated with a given statement, where $d = 1, \dots, D$;

$\theta_{d_A}, \dots, \theta_{d_D}$ = the respondent's latent trait scores on the respective dimensions;

$P_A(1), \dots, P_D(1)$ = the probabilities of endorsing statements A through D;

$P_A(0), P_D(0)$ = the probabilities of not endorsing statements A through D; and

$P_{(A>B,C,D)_i}(\theta_{d_A}, \theta_{d_B}, \theta_{d_C}, \theta_{d_D})$ = the probability of a respondent preferring statement A to statements B, C, and D in item tetrad i .

Similarly, letting TOTAL temporarily represent the denominator of (A1) for convenience, the probability of choosing statement B in the tetrad as *most like* is $P\{0,1,0,0\}/\text{TOTAL}$. The probability of choosing statement C as *most like* is $P\{0,0,1,0\}/\text{TOTAL}$, and the probability of choosing statement D as *most like* is $P\{0,0,0,1\}/\text{TOTAL}$.

To derive a general expression for HCM-PICK probabilities, the probability expressions for HCM observed disagree ($Z = 0$) and agree ($Z = 1$) responses must be substituted into the appropriate PICK model terms representing disagreement, $P_A(0)$, $P_B(0)$, $P_C(0)$, and $P_D(0)$, and agreement, $P_A(1)$, $P_B(1)$, $P_C(1)$, and $P_D(1)$, above.

According to Andrich and Luo (1993), HCM observed response probabilities are given by:

$$P[\text{Disagree}|\theta] = P[Z = 0|\theta] = \frac{2 \cosh(\theta - \delta)}{\exp(\tau) + 2 \cosh(\theta - \delta)}, \quad (\text{A2})$$

and

$$P[\text{Agree}|\theta] = P[Z = 1|\theta] = \frac{\exp(\tau)}{\exp(\tau) + 2 \cosh(\theta - \delta)}, \quad (\text{A3})$$

where θ represents a respondent's trait score on the dimension represented by the statement under consideration, δ is a statement location parameter that coincides with the peak of the Agree response function, and τ is a latitude of acceptance parameter, akin to discrimination, which denotes a region on either side of the peak where the probability of an Agree response is most likely. (See Chapter 3 for details.)

Next, to derive a compact general expression for HCM-PICK probabilities, it is helpful to define the cosh and exp terms involving statements A, B, C, and D symbolically. For

convenience and visual clarity, let A, B, C, and D now represent mathematical functions involving those statements, as follows:

$$\begin{aligned}
 A &= \cosh(\theta_{d_A} - \delta_A) \\
 B &= \cosh(\theta_{d_B} - \delta_B) \\
 C &= \cosh(\theta_{d_C} - \delta_C) \\
 D &= \cosh(\theta_{d_D} - \delta_D) \\
 T_A &= \exp(\tau_A) \\
 T_B &= \exp(\tau_B) \\
 T_C &= \exp(\tau_C) \\
 T_D &= \exp(\tau_D).
 \end{aligned} \tag{A4}$$

Substituting the expressions in (A4) into the numerator of (A1), we get:

$$\begin{aligned}
 P\{1,0,0,0\} &= \frac{T_A}{T_A+2A} * \frac{2B}{T_B+2B} * \frac{2C}{T_C+2C} * \frac{2D}{T_D+2D} = \\
 &= \frac{8T_A B C D}{[T_A+2A][T_B+2B][T_C+2C][T_D+2D]}.
 \end{aligned} \tag{A5}$$

Substituting the expressions in (A4) into the denominator of (A1), we get:

$$\begin{aligned}
 P\{1,0,0,0\} + P\{0,1,0,0\} + P\{0,0,1,0\} + P\{0,0,0,1\} &= \\
 &= \frac{8T_A B C D + 8A T_B C D + 8A B T_C D + 8A B C T_D}{[T_A+2A][T_B+2B][T_C+2C][T_D+2D]}.
 \end{aligned} \tag{A6}$$

Thus, a new expression for (A1) can be obtained by dividing (A5) by (A6) or, alternatively, multiplying (A5) by the reciprocal of (A6), as shown:

$$\frac{8T_A BCD}{[T_A+2A][T_B+2B][T_C+2C][T_D+2D]} * \frac{[T_A+2A][T_B+2B][T_C+2C][T_D+2D]}{8T_A BCD+8AT_B CD+8ABT_C D+8ABCT_D}, \quad (A7)$$

which simplifies to:

$$\frac{T_A BCD}{T_A BCD+AT_B CD+ABT_C D+ABCT_D}. \quad (A8)$$

Thus, compact general expressions for HCM-PICK probabilities corresponding to selecting statements A, B, C, and D, respectively, as *most like* are as follows:

$$P_{(A>B,C,D)}_i(\theta_{d_A}, \theta_{d_B}, \theta_{d_C}, \theta_{d_D}) = \frac{T_A BCD}{T_A BCD+AT_B CD+ABT_C D+ABCT_D} \quad (A9a)$$

$$P_{(B>A,C,D)}_i(\theta_{d_A}, \theta_{d_B}, \theta_{d_C}, \theta_{d_D}) = \frac{AT_B CD}{T_A BCD+AT_B CD+ABT_C D+ABCT_D} \quad (A9b)$$

$$P_{(C>A,B,D)}_i(\theta_{d_A}, \theta_{d_B}, \theta_{d_C}, \theta_{d_D}) = \frac{ABT_C D}{T_A BCD+AT_B CD+ABT_C D+ABCT_D} \quad (A9c)$$

$$P_{(D>A,B,C)}_i(\theta_{d_A}, \theta_{d_B}, \theta_{d_C}, \theta_{d_D}) = \frac{ABCT_D}{T_A BCD+AT_B CD+ABT_C D+ABCT_D}. \quad (A9d)$$

It can be seen in the expressions contained in (A9) that the numerator for each k option is the product of the exponent of τ_k and the hyperbolic cosine of $(\theta - \delta)$ for the non- k statements.

This numerator term for each k can be written using the product operator as:

$$\exp (\tau_k) \prod_{\substack{c=1 \\ c \neq k}}^M \cosh (\theta_{d_c} - \delta_c) \quad (\text{A10})$$

The denominator in the (A9) expressions is simply the sum of the numerators, which can be expressed via a summation operator over all M statements as:

$$\sum_{c=1}^M \left(\exp (\tau_c) \prod_{\substack{v=1 \\ v \neq c}}^M [\cosh (\theta_{d_v} - \delta_v)] \right) \quad (\text{A11})$$

Utilizing the numerator and denominator provided in (A10) and (A11) gives the general expression for *HCM-PICK* probabilities:

$$P_{k|b_i}(\theta_{d_1}, \dots, \theta_{d_M}) = \frac{\exp (\tau_k) \prod_{\substack{c=1 \\ c \neq k}}^M \cosh (\theta_{d_c} - \delta_c)}{\sum_{c=1}^M \left(\exp (\tau_c) \prod_{\substack{v=1 \\ v \neq c}}^M [\cosh (\theta_{d_v} - \delta_v)] \right)}, \quad (\text{A12})$$

where

i = the index for item blocks involving M statements, where $i = 1$ to I ;

k, c, v = index variables representing each successive term in a series;

\mathbf{b} = the set of statements included in a block;

d = the dimension associated with a given statement, where $d = 1, \dots, D$;

$\theta_{d_1}, \dots, \theta_{d_M}$ = the latent trait values for a respondent on dimensions d_1 to d_M ;

δ = the location parameter for a given statement;

τ = the latitude of acceptance parameter for a given statement; and

$P_{k|b_i}(\theta_{d_1}, \dots, \theta_{d_M})$ = the probability of a respondent selecting statement k as most like in the ith block of M statements.

APPENDIX B:

SINGLE-STATEMENT ITEM CONTENT FOR STUDY 1

Please indicate your level of agreement with each of the items below on the scale provided.

1	2	3	5
Strongly Disagree	Disagree	Agree	Strongly Agree

Statement	Dimension	Statement Content
1	Conscientiousness	I am incapable of planning ahead.
2	Conscientiousness	I do well on tasks requiring attention unless the task is really long.
3	Conscientiousness	I am really good at tasks that require a careful and cautious approach.
4	Conscientiousness	Setting goals and achieving them is not very important to me.
5	Conscientiousness	I work about as hard to complete tasks as most people I know.
6	Conscientiousness	I demand the highest quality in everything I do.
7	Conscientiousness	Clutter doesn't bother me in the least.
8	Conscientiousness	When it comes to being tidy and clean, I am about average.
9	Conscientiousness	I don't like things around me to be disorganized.
10	Conscientiousness	I don't consider being late for an appointment a big deal.
11	Conscientiousness	I keep promises about as often as others - no more, no less.
12	Conscientiousness	My friends know that they can count on me in times of need.
13	Conscientiousness	I believe it is important to do the right thing, even if some people might not like it.
14	Conscientiousness	It's okay to exaggerate a little during a job interview, but I would never tell an outright lie.
15	Conscientiousness	I have high standards and work toward them.
16	Conscientiousness	I tend to have almost no clutter on my work desk or in my home.
17	Conscientiousness	I have always felt an extremely strong sense of personal responsibility and duty.
18	Conscientiousness	I won't seriously consider breaking the rules, even if I know I can.

19	Conscientiousness	After being distracted, it takes a long time for me to get my concentration back.
20	Conscientiousness	Most of the time I am pretty careful, but when I am in a real hurry, I can be a bit reckless.
21	Conscientiousness	I think twice before agreeing to do something.
22	Conscientiousness	I tend to set goals that are challenging, but still reachable.
23	Conscientiousness	Keeping things organized does not come naturally to me, but I try anyway.
24	Conscientiousness	Sometimes it is too much of a bother to do exactly what I promised.
25	Conscientiousness	I am usually not the most responsible member of a group, but I don't try to avoid my duties either.
26	Conscientiousness	I do not intend to follow every little rule that others make up.
27	Conscientiousness	If I found a sizeable amount of money, I'd keep it for myself and wouldn't worry about finding the owner.
28	Conscientiousness	I think it's okay to lie if you have a good reason for doing so.
29	Conscientiousness	If a cashier forgot to charge me for an item, I would let him or her know.
30	Conscientiousness	I am always prepared.
31	Conscientiousness	I pay attention to details.
32	Conscientiousness	I get chores done right away.
33	Conscientiousness	I carry out my plans.
34	Conscientiousness	I make plans and stick to them.
35	Conscientiousness	I complete tasks successfully.
36	Conscientiousness	I waste my time.
37	Conscientiousness	I find it difficult to get down to work.
38	Conscientiousness	I do just enough work to get by.
39	Conscientiousness	I don't see things through.
40	Conscientiousness	I shirk my duties.
41	Conscientiousness	I mess things up.
42	Emotional Stability	I worry about things no more or less than others.
43	Emotional Stability	I really worry about what others think of me.
44	Emotional Stability	I tend to get upset when others critique my work.
45	Emotional Stability	I can prevent negative emotions from interfering with my performance better than most people.
46	Emotional Stability	To make me really angry, someone would have to provoke me intentionally and do so more than once.
47	Emotional Stability	I tend to get annoyed easily.
48	Emotional Stability	Even when things don't go my way, I remain calm and composed.
49	Emotional Stability	It's not easy to make me angry.

50	Emotional Stability	Even when something bad happens, I can push negatives out of my mind.
51	Emotional Stability	I don't often feel sad, but when I do, I cheer up easily.
52	Emotional Stability	When someone criticizes me or my work, I withdraw and avoid everyone for a while.
53	Emotional Stability	I have a positive outlook on life.
54	Emotional Stability	If I do something stupid or embarrass myself, I usually just laugh it off.
55	Emotional Stability	I handle even the most stressful situations pretty well.
56	Emotional Stability	Because I constantly worry about things, it is hard for me to relax.
57	Emotional Stability	Even during a particularly heated argument, I keep my emotions under control.
58	Emotional Stability	Most people would say I have a hot temper.
59	Emotional Stability	I am relaxed most of the time.
60	Emotional Stability	I seldom feel blue.
61	Emotional Stability	I am not easily bothered by things.
62	Emotional Stability	I rarely get irritated.
63	Emotional Stability	I seldom get mad.
64	Emotional Stability	I get irritated easily.
65	Emotional Stability	I get stressed out easily.
66	Emotional Stability	I worry about things.
67	Emotional Stability	I am easily disturbed.
68	Emotional Stability	I get upset easily.
69	Emotional Stability	I change my mood a lot.
70	Emotional Stability	I have frequent mood swings.
71	Extraversion	I usually let other people get their way.
72	Extraversion	I can provide criticism if someone asks for it.
73	Extraversion	I like being in control of situations.
74	Extraversion	I would prefer not to be a leader.
75	Extraversion	People would call me a homebody.
76	Extraversion	I like to have a good time, but being the center of attention makes me uncomfortable.
77	Extraversion	I cannot stand being bored.
78	Extraversion	I crave action and excitement.
79	Extraversion	Meeting new people makes me nervous.
80	Extraversion	I don't go out of my way to meet people, but I make friends easily.
81	Extraversion	I strike up casual conversations easily.
82	Extraversion	I feel comfortable with my friends, but not always with new people.
83	Extraversion	I am a pushover.

84	Extraversion	I'm not comfortable ordering people around, but I can do it if I have to.
85	Extraversion	Sometimes I can persuade my friends to do things my way.
86	Extraversion	I'll take charge if no one else is willing to.
87	Extraversion	I want to succeed.
88	Extraversion	I can be very persuasive.
89	Extraversion	I like to take on leadership roles.
90	Extraversion	It's like pulling teeth to get me to go to a party.
91	Extraversion	I don't like to take risks.
92	Extraversion	I can be too cautious.
93	Extraversion	I like to go out, but I don't always feel like it.
94	Extraversion	Every once in awhile, I really want to do something risky and fun.
95	Extraversion	I like to go out anytime, not just on the weekends.
96	Extraversion	I can be pretty awkward around people.
97	Extraversion	I tend to be a very private person.
98	Extraversion	I prefer to avoid large parties.
99	Extraversion	I don't start conversations, but I'll talk to most people if they talk to me first.
100	Extraversion	I enjoy talking to strangers.
101	Extraversion	I meet new friends all the time.
102	Extraversion	I am the life of the party.
103	Extraversion	I feel comfortable around people.
104	Extraversion	I start conversations.
105	Extraversion	I talk to a lot of different people at parties.
106	Extraversion	I don't mind being the center of attention.
107	Extraversion	I make friends easily.
108	Extraversion	I don't talk a lot.
109	Extraversion	I keep in the background.
110	Extraversion	I have little to say.
111	Extraversion	I don't like to draw attention to myself.
112	Extraversion	I am quiet around strangers.
113	Extraversion	I find it difficult to approach others.
114	Openness	I enjoy looking at paintings just as much as the average person.
115	Openness	Music inspires and motivates me.
116	Openness	I'll willing to learn new things if they have some practical value.
117	Openness	I love to learn new things.
118	Openness	I can't stand getting caught up in theoretical discussions.
119	Openness	To me, personal growth is more important than money or

		personal recognition.
120	Openness	I think there's such a thing as "too much" imagination.
121	Openness	I like to try out new ways of doing things.
122	Openness	My solutions are pretty standard.
123	Openness	New ideas are hard for me to follow.
124	Openness	Sometimes it's tough to grasp new concepts at first, but I get them after awhile.
125	Openness	I can handle most challenging problems, but some take a lot of effort.
126	Openness	I'd like to attend public lectures on interesting topics.
127	Openness	I'm interested in how machines work.
128	Openness	I sometimes have trouble deciding if my ideas are good enough to give them a shot.
129	Openness	I have some pretty clever ideas.
130	Openness	I have a wild imagination.
131	Openness	I tend to pick up new skills and tricks easily.
132	Openness	I have trouble understanding instructions.
133	Openness	I tend to grasp new ideas quickly.
134	Openness	I just seem to know a lot.
135	Openness	I don't care much about nature's beauty.
136	Openness	I don't see the point in things like poetry.
137	Openness	As long as it gets me from A to B, I don't really care how my car works.
138	Openness	I can be persuaded to try some new things, but I can be reluctant.
139	Openness	I'm always interested in learning more about science and nature.
140	Openness	I like to read a lot.
141	Openness	I don't believe in changing horses mid-stream.
142	Openness	I stick with what works.
143	Openness	Nothing excites me like coming up with new ways to do things.
144	Openness	If we're stuck, I'll probably come up with some way to get out of it.
145	Openness	Maps sometimes confuse me.
146	Openness	Things don't come as easily for me as for others, but I am confident I can learn just about anything.
147	Openness	When I don't get a new idea right away, I just work a little harder and eventually get it.
148	Openness	I enjoy learning about other cultures and religions.
149	Openness	I believe in the importance of art.
150	Openness	I have a vivid imagination.

151	Openness	I enjoy wild flights of fantasy.
152	Openness	I carry the conversation to a higher level.
153	Openness	I enjoy hearing new ideas.
154	Openness	I enjoy thinking about things.
155	Openness	I am not interested in abstract ideas.
156	Openness	I do not like art.
157	Openness	I avoid philosophical discussions.
158	Openness	I do not enjoy going to art museums.
159	Openness	I am not interested in theoretical discussions.
160	Openness	I have difficulty understanding abstract ideas.

APPENDIX C:

SINGLE-STATEMENT IPIP ITEM CONTENT FOR STUDY 3

Please indicate your level of agreement with each of the items below on the scale provided.

1	2	3	5
Strongly Disagree	Disagree	Agree	Strongly Agree

Statement	Dimension	Statement Content
1	Conscientiousness	I am always prepared.
2	Conscientiousness	I pay attention to details.
3	Conscientiousness	I get chores done right away.
4	Conscientiousness	I carry out my plans.
5	Conscientiousness	I make plans and stick to them.
6	Conscientiousness	I complete tasks successfully.
7	Conscientiousness	I waste my time.
8	Conscientiousness	I find it difficult to get down to work.
9	Conscientiousness	I do just enough work to get by.
10	Conscientiousness	I don't see things through.
11	Conscientiousness	I shirk my duties.
12	Conscientiousness	I mess things up.
13	Emotional Stability	I am relaxed most of the time.
14	Emotional Stability	I seldom feel blue.
15	Emotional Stability	I am not easily bothered by things.
16	Emotional Stability	I rarely get irritated.
17	Emotional Stability	I seldom get mad.
18	Emotional Stability	I get irritated easily.
19	Emotional Stability	I get stressed out easily.
20	Emotional Stability	I worry about things.
21	Emotional Stability	I am easily disturbed.
22	Emotional Stability	I get upset easily.
23	Emotional Stability	I change my mood a lot.
24	Emotional Stability	I have frequent mood swings.
25	Extraversion	I am the life of the party.
26	Extraversion	I feel comfortable around people.

27	Extraversion	I start conversations.
28	Extraversion	I talk to a lot of different people at parties.
29	Extraversion	I don't mind being the center of attention.
30	Extraversion	I make friends easily.
31	Extraversion	I don't talk a lot.
32	Extraversion	I keep in the background.
33	Extraversion	I have little to say.
34	Extraversion	I don't like to draw attention to myself.
35	Extraversion	I am quiet around strangers.
36	Extraversion	I find it difficult to approach others.
37	Openness	I believe in the importance of art.
38	Openness	I have a vivid imagination.
39	Openness	I enjoy wild flights of fantasy.
40	Openness	I carry the conversation to a higher level.
41	Openness	I enjoy hearing new ideas.
42	Openness	I enjoy thinking about things.
43	Openness	I am not interested in abstract ideas.
44	Openness	I do not like art.
45	Openness	I avoid philosophical discussions.
46	Openness	I do not enjoy going to art museums.
47	Openness	I am not interested in theoretical discussions.
48	Openness	I have difficulty understanding abstract ideas.

APPENDIX D:

4-D MFC TETRAD MEASURE FOR STUDY 3

Block	Dimension	Statement Content
1	Conscientiousness	I am incapable of planning ahead.
	Emotional Stability	I really worry about what others think of me.
	Extraversion	I usually let other people get their way.
	Openness	I can't stand getting caught up in theoretical discussions.
2	Conscientiousness	Setting goals and achieving them is not very important to me.
	Emotional Stability	When someone criticizes me or my work, I withdraw and avoid everyone for a while.
	Extraversion	I would prefer not to be a leader.
	Openness	New ideas are hard for me to follow.
3	Conscientiousness	Clutter doesn't bother me in the least.
	Emotional Stability	I tend to get upset when others critique my work.
	Extraversion	People would call me a homebody.
	Openness	I think there's such a thing as "too much" imagination.
4	Conscientiousness	I don't consider being late for an appointment a big deal.
	Emotional Stability	I tend to get annoyed easily.
	Extraversion	Meeting new people makes me nervous.
	Openness	I'll willing to learn new things if they have some practical value.
5	Conscientiousness	I do well on tasks requiring attention unless the task is really long.
	Emotional Stability	I worry about things no more or less than others.
	Extraversion	I like to have a good time, but being the center of attention makes me uncomfortable.
	Openness	I can handle most challenging problems, but some take a lot of effort.
6	Conscientiousness	I work about as hard to complete tasks as most people I know.
	Emotional Stability	Even when something bad happens, I can push negatives out of my mind.
	Extraversion	I can provide criticism if someone asks for it.
	Openness	I enjoy looking at paintings just as much as the average person.
7	Conscientiousness	When it comes to being tidy and clean, I am about average.

	Emotional Stability	To make me really angry, someone would have to provoke me intentionally and do so more than once.
	Extraversion	I don't go out of my way to meet people, but I make friends easily.
	Openness	My solutions to problems are pretty standard.
8	Conscientiousness	I keep promises about as often as others.
	Emotional Stability	I don't often feel sad, but when I do, I cheer up easily.
	Extraversion	I feel comfortable with my friends, but not always with new people.
	Openness	Sometimes it's tough to grasp new concepts at first, but I get them after awhile.
9	Conscientiousness	I am really good at tasks that require a careful and cautious approach.
	Emotional Stability	Even when things don't go my way, I remain calm and composed.
	Extraversion	I strike up casual conversations easily.
	Openness	Music inspires and motivates me.
10	Conscientiousness	I don't like things around me to be disorganized.
	Emotional Stability	It's not easy to make me angry.
	Extraversion	I like being in control of situations.
	Openness	I love to learn new things.
11	Conscientiousness	My friends know that they can count on me in times of need.
	Emotional Stability	I can prevent negative emotions from interfering with my performance better than most people.
	Extraversion	I cannot stand being bored.
	Openness	To me, personal growth is more important than money or personal recognition.
12	Conscientiousness	I demand the highest quality in everything I do.
	Emotional Stability	I have a positive outlook on life.
	Extraversion	I crave action and excitement.
	Openness	I like to try out new ways of doing things.
